



Calhoun: The NPS Institutional Archive

Theses and Dissertations

Thesis and Dissertation Collection

1965

Computer simulation for the comparison of ASW vehicles

Dougherty, William A., Jr.

Monterey, California. Naval Postgraduate School

<http://hdl.handle.net/10945/24637>



Calhoun is a project of the Dudley Knox Library at NPS, furthering the precepts and goals of open government and government transparency. All information contained herein has been approved for release by the NPS Public Affairs Officer.

Dudley Knox Library / Naval Postgraduate School
411 Dyer Road / 1 University Circle
Monterey, California USA 93943

<http://www.nps.edu/library>

NPS ARCHIVE
1965
DOUGHERTY, W.

COMPUTER SIMULATION FOR THE
COMPARISON OF ASW VEHICLES

WILLIAM A. DOUGHERTY.

COMPUTER SIMULATION FOR THE COMPARISON
OF ASW VEHICLES

by

William A. Dougherty, Jr.
Lieutenant, United States Navy

Submitted in partial fulfillment of
the requirements for the degree of

MASTER OF SCIENCE
IN
OPERATIONS RESEARCH

United States Naval Postgraduate School
Monterey, California

1 9 6 5

COMPUTER SIMULATION FOR THE COMPARISON
OF ASW VEHICLES

by

William A. Dougherty, Jr.

This work is accepted as fulfilling
the thesis requirements for the degree of
MASTER OF SCIENCE
IN
OPERATIONS RESEARCH
from the
United States Naval Postgraduate School

ABSTRACT

A method is developed to analyze and compare the effectiveness of ASW vehicles. The measure of effectiveness is the probability that the vehicle, after detecting a submarine with passive sensors, can transit to the contact area and re-establish contact with the submarine. A computer simulation is developed and an example using three hypothetical ASW vehicles is illustrated.

TABLE OF CONTENTS

Section	Title	Page
1.	Introduction	1
2.	Simulation Description and Mathematical Development	3
3.	Input Data Rules	18
4.	An Example and Some Applications	22
5.	Conclusions	29
6.	Bibliography	31
Appendix		
A.	Glossary	32
B.	Flow Charts	35
C.	Computer Program	45

LIST OF ILLUSTRATIONS

Figure		Page
1.	The Maneuvering Board Solution	5
2.	Numerical Integration for the Unalerted Case	9
3.	Alerted Case	13
4.	Input Data Procedure	19
5.	Input Parameter Set	23
6.	Probability Output	24
7.	Curves for the High Speed Surface Vehicle	25
8.	Curves for the VERTOL Vehicle	26
9.	Curves for the SEAPLANE Type Vehicle	27

1. Introduction.

As a result of increased emphasis currently being placed on ASW weapon systems, it is advantageous to possess a computer simulation capable of analyzing and comparing proposed ASW vehicles and operational ASW vehicles. The computer simulation for the comparison of ASW vehicles developed in this paper is intended to be used for this purpose.

The problem at hand is to develop a method for comparing ASW vehicles under operational conditions using vehicle, submarine, and tactical situation parameters. The simulation allows one to compute a probability which is used as a measure of effectiveness. This probability, hereafter referred to as the "probability of success," is defined in this paper as the probability that an ASW vehicle successfully relocates a submarine at an estimated position given that a detection has occurred.

A description of the simulation and its limitations is made in Section 2. It is very important to understand the simulation and the background assumptions before the results of the simulation are analyzed. After the problem is developed mathematically in Section 2, a discussion and an illustration is given in Section 3 to demonstrate how to use the computer program. In Section 4, several applications are discussed. Finally a comparison is made of three hypothetical ASW vehicles--a High Speed Surface Vehicle, a VERTOL Vehicle, and a Seaplane-Type Vehicle--using the results generated from the computer simulation. The output of one computer run is illustrated in Figures 5 and 6. Curves for the probability of success versus range to the submarine for each vehicle are displayed in Figures 7, 8, and 9. These curves are used to analyze and compare the systems.

The results of these comparisons illustrate the usefulness of the simulation in comparing the performance of different vehicles and for studying the effect of various parameters such as expected sensor range on the probability of success.

2. Simulation Description and Mathematical Development.

Effort has been directed toward the development of a computer simulation that represents a real world conflict between an ASW vehicle and a submarine. The setting is one of an ASW vehicle assigned to a patrol, surveillance, or barrier mission. Initial detection is assumed to have been made using passive sensors. The vehicle then proceeds as rapidly as possible to an estimated position (EP) in order to relocate the submarine. The EP is the predicted position of the submarine when the actual position is not known, but the vehicle's sensors indicate the presence of a submarine. The objective of the vehicle is to compute an EP of the submarine, close the position at maximum speed, and attempt to relocate the submarine using active sensors. No information about the actions of the submarine is available while the vehicle closes to the EP.

Certain other restrictions are assumed in the model. Ahead thrown weapons and nuclear weapons are not available for use by the vehicle. Multiple targets are excluded. A passive detection range of at least five nautical miles is necessary; otherwise, an active sensor would be used and the problem of transiting to an estimated position is irrelevant. Also, the vehicle is assumed to lie motionless in the water until detection has been achieved to insure passive sensor capability.

The simulation is developed for two different tactical situations. The first case is that of a submarine which is unaware of the activity of the vehicle. The second case is that of a submarine which is alerted by the activity of the vehicle. Common to both of these cases is a maneuvering board problem which will be discussed first.

The maneuvering board solution consists of describing geometrically the positions and motions of a vehicle and a submarine with time. The passive sensor of the vehicle provides the last known position, course and speed of the submarine, and the bearing and range to the submarine from the vehicle. Knowing these values and the vehicle speed, an EP, transit time of the vehicle, relative closing speed, and the distance traveled to EP are computed. For overall ease in reading the same notation is used in the mathematical development that has been used in the computer simulation (Appendix C).

The solution is computed by solving a velocity vector problem. The vehicle is located at the origin (0,0) of a rectangular coordinate system. One side of the velocity triangle (Figure 1) represents the estimated velocity vector of the submarine (U_1) which is re-established at the origin. The velocity vector for the vehicle (Z) is unknown in direction, but known in magnitude. The remaining relative velocity vector (RELSPD) represents the relative course and speed of the vehicle closing the submarine. Only the direction of RELSPD is known which is parallel to the true bearing line from the vehicle at (0,0) to the submarine at (X_2, Y_2). Then the intersection (X_3, Y_3) between the relative velocity vector and the vehicle velocity circle is computed.

In order to solve the maneuvering board problem various points and vectors in the rectangular coordinate system must be computed. The values for the components of U_1 are:

$$X_1 = U_1 \times \sin (\text{THETA}) \quad (1)$$

$$Y_1 = U_1 \times \cos (\text{THETA}) \quad (2)$$

The last known position (X_2, Y_2) of the submarine is given by:

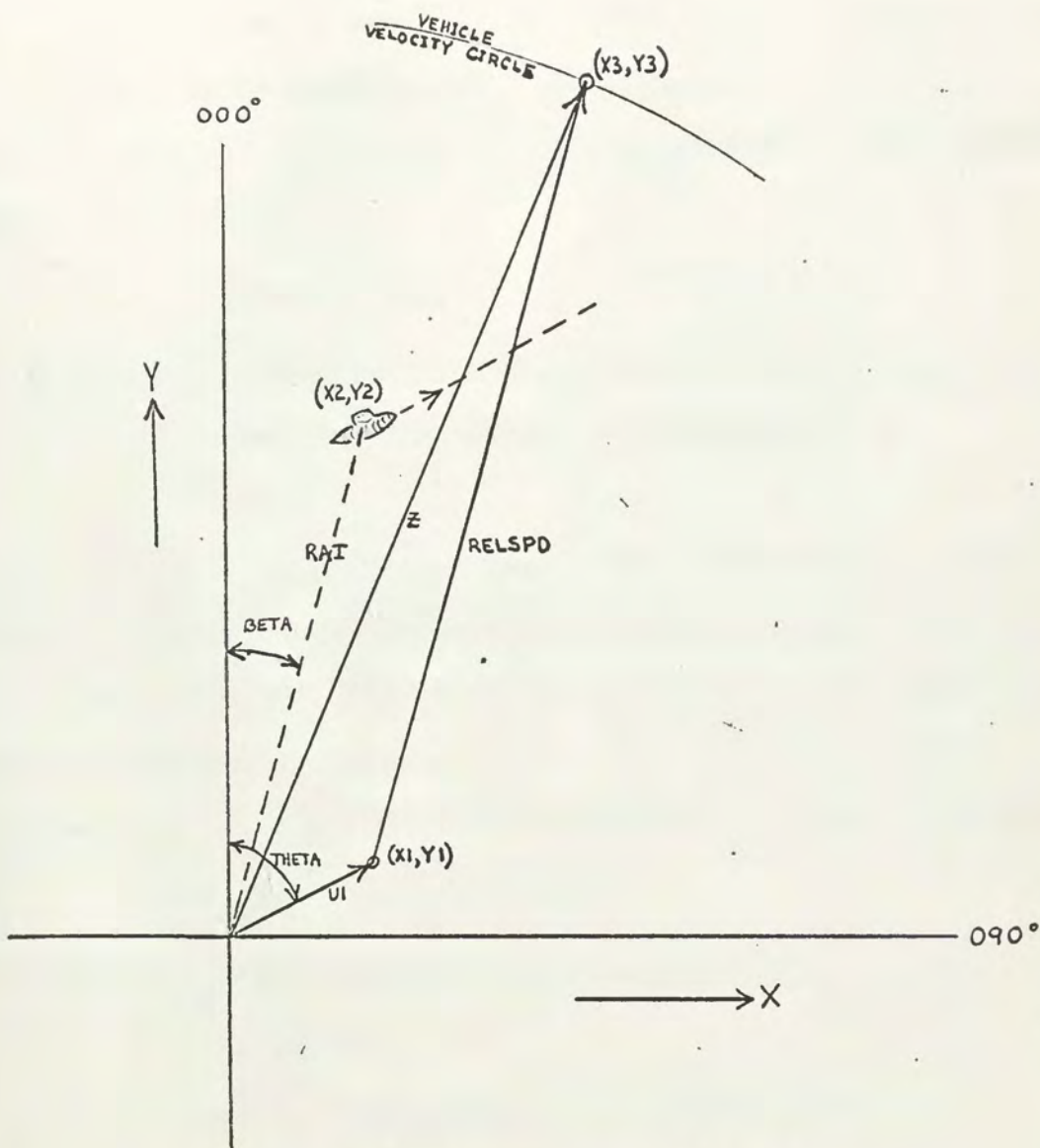


Figure 1. The Maneuvering Board Solution

$$X2 = RAI \times \sin (BETA) \quad (3)$$

$$Y2 = RAI \times \cos (BETA) , \quad (4)$$

where BETA is the bearing in degrees of the submarine from the vehicle and RAI is the range in nautical miles of the submarine from the vehicle. The RELSPD vector is represented by the line through the point (X1, Y1) and parallel to the line connecting the origin and (X2, Y2). The equation of this line is:

$$Y3 = \frac{Y2}{X2} (X3 - X1) + Y1 . \quad (5)$$

The RELSPD vector intersects the vehicle velocity circle at the point (X3, Y3). The equation of the vehicle velocity circle is:

$$Y3^2 + X3^2 = V^2 , \quad (6)$$

where V is the average vehicle transit speed. The point (X3, Y3) is determined by solving equations (5) and (6) simultaneously. The direction of the vector from the origin to (X3, Y3) represents the course of the vehicle when traveling inbound to EP. The relative speed vector is represented by the vector between (X1, Y1) and (X3, Y3) and its magnitude is:

$$RELSPD = \sqrt{(X3 - X1)^2 + (Y3 - Y1)^2} . \quad (7)$$

The vehicle's transit time (TD) to EP is defined as:

$$TD = RAI / RELSPD . \quad (8)$$

Let the vehicle reaction time (RT) be the following sum:

$$RT = PTOT + TOT + CLOT + RELT , \quad (9)$$

where , PTOT - pretake-off time which commences when the vehicle can no longer observe the submarine and includes decision time, warm-up time, and sensor retrieval time,

TOT - take-off time which includes take-off roll and time to take-off into the wind,

CLOT - land time which includes time to land and taxi time needed to arrive at EP in order to deploy active sensors,

RELT - target relocation time which includes the time necessary to deploy sensors and ends when the submarine is re-located.

Any of these times can have a zero value. For example, a helicopter could have TOT equal to zero if it needs no take-off time. Also, the times are mutually exclusive so that no time interval is added twice. Obviously the blind time (TB) is:

$$TB = RT + TD. \quad (10)$$

Evasion for the alerted submarine begins when blind time commences. At that time the submarine is assumed to be at (X2, Y2). If RT is equal to zero, the submarine is at (X2, Y2) when evasion begins; but if RT is not equal to zero, the submarine is not actually at (X2, Y2) when evasion begins because it takes RT for the vehicle to commence moving towards EP. During the reaction time the vehicle is motionless, but the submarine is moving away from (X2, Y2). Because of the small displacement of the submarine from (X2, Y2) due to RT, the assumption that the submarine is at (X2, Y2) when evasion begins does not significantly affect the results of the simulation.

It is necessary to determine the estimated position (EP) of the submarine after a time interval of TB and a submarine speed U3. The equation of the estimated distance (DIST) traveled by the submarine is:

$$DIST = U3 \times TB. \quad (11)$$

The EP is also the position at which the vehicle estimates that an intercept will be made with the submarine. The components of EP relative to the origin are:

$$X4 = DIST \times \sin (\text{THETA}) + X2 \quad (12)$$

$$Y_4 = \text{DIST} \times \cos(\text{THETA}) + Y_2. \quad (13)$$

The equation for the distance DISDAT) traveled by the vehicle to EP is

$$\text{DISDAT} = \sqrt{X_4^2 + Y_4^2}. \quad (14)$$

The values for TB and DIST are very important in determining the probabilities of success for the two cases developed below.

Case I. The unalerted submarine:

It is conceivable that the vehicle could transit to EP without the submarine being cognizant of the impending danger. In this case the unalerted submarine does not evade and proceeds at cruise course and velocity. Prediction errors for the submarine course and velocity are made which are characteristic of the vehicle's equipment. The errors are assumed to be distributed normally about the predicted course and velocity. Because of long blind times expected, the predicted positions of the submarine are not accurately represented by a circular-normal distribution, and a numerical integration must be performed. Probabilities of success are computed for each of a representative distribution of predicted positions consisting of 25 points or cells (see Figure 2). This concept has been adopted from [3].

The last known submarine position (X2, Y2) is established at the origin of a rectangular coordinate system. Since DIST is the distance traveled by the submarine during TB, then EP is (DIST,0) in this coordinate system.

Using the prediction errors, a submarine position is computed for each of the 25 cell midpoints. The distance (VV) and angle (THETER) for each cell are computed using the submarine cruise speed (U1), the submarine

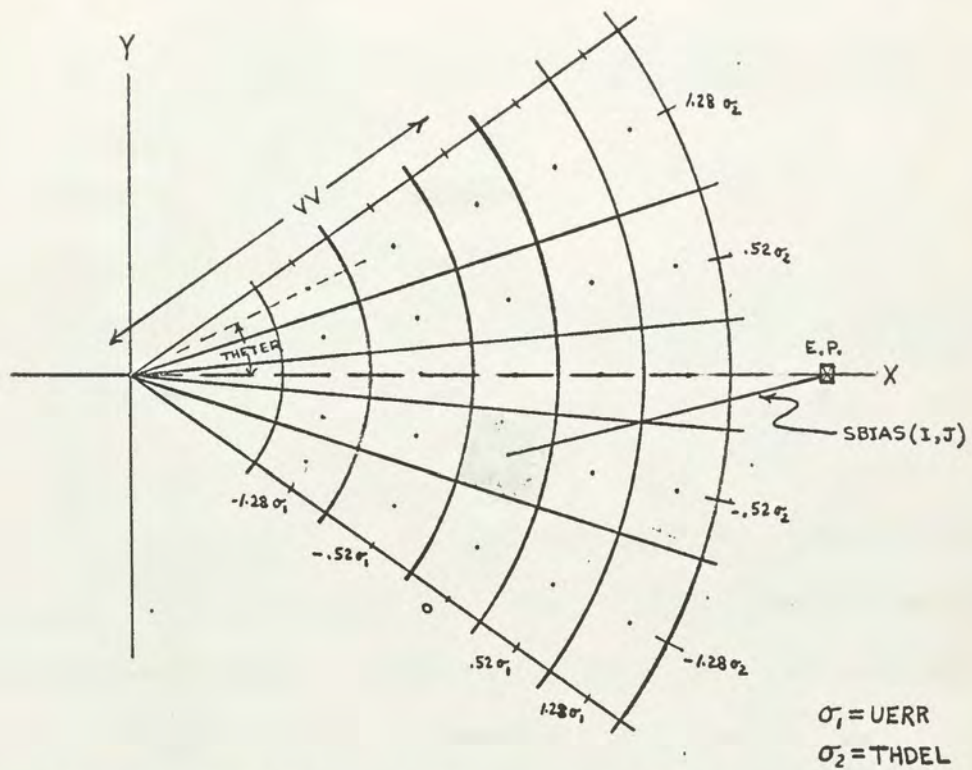


Figure 2 Numerical Integration For The Unaltered Case

speed error (UERR), the submarine course error (THDEL), and the blind time (TB). The equations for VV and THETER are:

$$VV = (U1 - AA(I) \times UERR) \times TB \quad (15)$$

$$THETER = AA(J) \times THDEL, \quad (16)$$

with $AA(I)$ and $AA(J) = 0, \pm .52, \pm 1.28$ depending on which cell is being considered. These numbers can be obtained from any normal density tables, [2].

The equations for the submarine position (SUBX (I,J), SUBY(I,J)) at the center of each of the 25 cells are:

$$SUBX(I,J) = VV \times \cos(THETER) \quad (17)$$

$$SUBY(I,J) = VV \times \sin(THETER). \quad (18)$$

A bias is computed between EP and the center of each cell. The equation for the bias of the (i,j)th cell is:

$$SBIAS(I,J) = \sqrt{(SUBX(I,J) - DIST)^2 + (SUBY(I,J))^2}. \quad (19)$$

Various errors have to be considered to give the simulation realism. It is assumed that the navigation error and sensor locating error are additive about the point EP. The distribution of the vehicle location about EP due to these errors is assumed to be circular normal.

The standard deviation of navigation error (SIGNAV) is:

$$SIGNAV = PRCNTN \times RAI \quad (20)$$

where PRCNTN is a percentage of the last known range (RAI). The standard deviation of sensor locating error consists of the standard deviation of bearing (SIGSBR) and the standard deviation of range (SIGSR) which are defined by:

$$SIGSR = PRCNTS \times RAI \quad (21)$$

$$SIGSBR = RAI \times \sin(BRGER) \quad (22)$$

where BRGER is the bearing error and PRCNTS is the percentage error of the last known range. Since (21) is greater than (22), because of the passive sensor, an elliptical normal distribution exists; but it is approximated by a circular normal distribution for ease of computation. This is accomplished by equating the area of an ellipse to the area of a circle. The result is an approximate standard deviation (SIGAPR).

$$\pi \sigma_{XE} \sigma_{YE} = \pi \sigma_{CIR}^2, \text{ with } \sigma_{XE} = \text{SIGSBR} \quad (23)$$

$$\sigma_{YE} = \text{SIGSR}$$

$$\therefore \text{SIGAPR} = \sigma_{CIR} = \sqrt{\sigma_{XE} \sigma_{YE}} \quad (24)$$

Therefore, the total standard deviation of error (SIGJT) is the sum of the squares of the approximate standard deviation of error and the standard deviation of navigation error according to the equation:

$$\text{SIGJT} = \sqrt{(\text{SIGNAV})^2 + (\text{SIGAPR})^2} \quad (25)$$

Other error models were considered in order to more accurately represent the errors involved. Due to lack of time the error model described above, although not the best, was adopted.

To compute the probability of success for the unalerted submarine the circular coverage function is used, [1]. In order to use this function, the parameters SBIAS(I,J), SIGJT, and EXPRNG are required. The first two have been defined above. The term EXPRNG, which is defined as the expected range of the active sensor used by the vehicle, is a characteristic of the sensor employed. The quantities $\frac{\text{SBIAS(I,J)}}{\text{SIGJT}}$ and

$\frac{\text{EXPRNG}}{\text{SIGJT}}$ are used in the circular coverage function to compute the probability of success (PK(I,J)) that a circular disk of radius EXPRNG will

cover a point (SUBX(I,J), SUBY(I,J)) from the EP since the probable position of the disk is described by a Gaussian distribution. This probability PK(I,J) is the probability of success for the ijth cell. Since it is equally likely that the submarine is in each of the 25 cells, the probability that it is within each cell is .04. The probabilities of success for each cell are summed and multiplied by .04 to give the "probability of success (PROB) against an unalerted submarine." The probability of success is:

$$\text{PROB} = \sum_I \sum_J (\text{PK}(I,J) \times .04) \quad (26)$$

Case II. The alerted submarine:

The submarine is aware of the presence of an ASW vehicle and evades by changing course and speed. The speed changes are characteristics of the submarine but the course changes are determined in number and degree by the situation being simulated. A probability of success is computed for each evasion turn and an arithmetic average taken over the number of evasion tactics used.

This case is designed to give practically full evasion to the submarine (see Figure 3). The submarine evasion turns are limited to a maximum turn of 90 degrees to either side of the estimated submarine course. No additional turns are granted after the initial turn is executed. For turns greater than 90 degrees the submarine would deviate from its initial track to such an extent that it would not be able to make up the lost time necessary to make good a mission speed of advance.

The range of values for the set of evasion turns is determined by the situation being simulated. For example, a slow submarine would

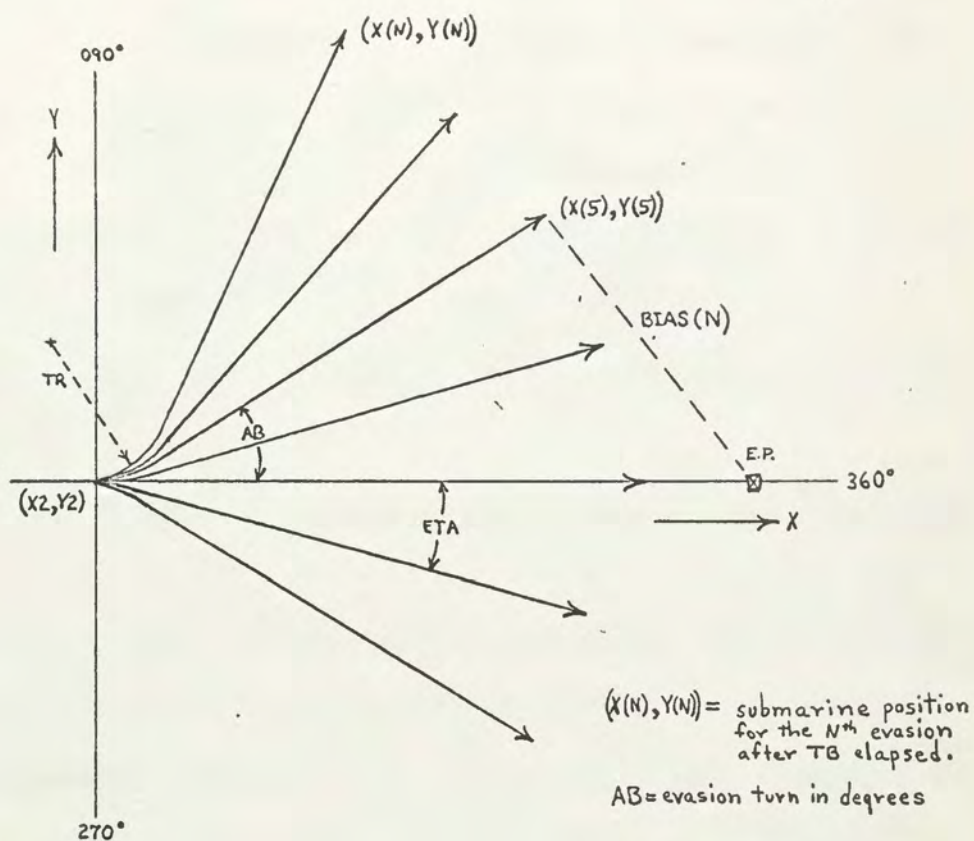


Figure 3 Alerted Case

almost always turn away from the vehicle when the vehicle's presence is known. There are two limiting turns which bound the set of evasion turns to the right and the left. The bounds must be no greater than 90 degrees to either side of the estimated submarine course. PSI and DELTA are the left bound and right bound, respectively. The range of values for the set of evasion turns is determined by (PSI-DELTA). The interval (ETA) between evasion turns is $ETA = \frac{PSI-DELTA}{NU}$, NU being the number of evasion turns considered. If the set of turns encompasses turns to the right of the submarine course then $ETA = \frac{PSI (360-DELTA)}{NU}$. In Figure 3, PSI = 060 degrees, DELTA = 330°, and $ETA = \frac{060 (360-330)}{6} = 15^\circ$. Therefore, the evasion turns considered for this example are 330°, 345°, 360°, 015°, 030°, 045°, and 060°.

In the alerted submarine case the submarine course and velocity prediction errors that were present in the unalerted case are ignored. Since in this case a set of evasion turns are selected which are only subjective predictions, it is valid to exclude prediction errors because they are comparatively insignificant to the computations. However, vehicle sensor and navigation errors that were assumed in the unalerted case still prevail.

Initially, the submarine is at cruise speed. When evasion commences, the assumed submarine speed is increased to fast speed. The characteristics of the submarine determine how long the submarine remains at fast speed (length of time is T1) after which it slows to silent speed. The time intervals of acceleration and deceleration are considered negligible when compared with the long blind times encountered.

The alerted case uses a rectangular coordinate system with the last

known position of the submarine (X2,Y2) at the point of origin when evasion begins. From this point positions (X(N), Y(N)), which are the positions at the end of each of the N evasion turns, are calculated. (See Figure 3.) The time to turn (TTT), evasion turn in degrees (AB), and the turning radius (TR) are needed to compute X(N) and Y(N). The equations for TTT, X(N), and Y(N) are computed as follows:

$$TTT = \frac{\text{arc length}}{\text{sub speed}} = \frac{TR \times AB}{U3}$$

If $TI \geq TB$, then

$$X(N) = TR \times \sin(AB) + U3 \times (TB - TTT) \cos(AB) \quad (27)$$

$$Y(N) = TR - TR \times \cos(AB) + U3 \times (TB - TTT) \sin(AB) . \quad (28)$$

If $TI < TB$, then

$$X(N) = TR \times \sin(AB) + U3 \times (TB - TTT) \cos(AB) + (TB - T1)U2 \times \cos(AB) \quad (29)$$

$$Y(N) = TR - TR \times \cos(AB) + U3 \times (TB - TTT) \sin(AB) + (TB - T1)U2 \times \sin(AB) . \quad (30)$$

The time T1 is the length of time the submarine remains at fast speed (U3); after which it changes to silent speed (U2). Equations (29) and (30) account for the speed change occurring before TB has terminated. The point (X(N),Y(N)) can be considered the submarine's actual position after the Nth evasion turn is taken.

The estimated position EP is the predicted position of the submarine after the interval of blind time has elapsed. Therefore, EP is (DIST,0). The distance between each (X(N),Y(N)) and EP constitutes a bias (BIAS(N)). This is an important factor in computing the probability of success. The bias for the Nth evasion turn is:

$$BIAS(N) = \sqrt{(X(N) - DIST)^2 + (Y(N))^2} . \quad (31)$$

As in the unalerted case, the parameters BIAS, EXPRNG, and SIGJT must be

computed (EXPRNG and SIGJT are the same as in the unalerted case) in order to use the circular coverage function. The circular coverage function is used to compute the probability (PPK(N)), for each N, that the vehicle can regain contact at EP given the total standard deviation of error (SIGJT), the bias (BIAS(N)) between the terminal point of the Nth evasion and EP, and the expected active sonar range (EXPRNG).

The two ratios of the parameters that are needed for the circular coverage function are $\frac{\text{BIAS}(N)}{\text{SIGJT}}$ and $\frac{\text{EXPRNG}}{\text{SIGJT}}$. With these ratios the probabilities, PPK(N), are computed for each N, and then all PPK(N), N = 1, ..., NU+1, are summed and averaged over all NU+1. The average probability is:

$$\text{PAVG} = \frac{\sum_{N=1}^{NU+1} \text{PPK}(N)}{NU+1} \quad (32)$$

It might be appropriate to use the option to weight each of the evasion turns. If it is believed that the turns within the set of evasion turns are not equally likely, then the probability vector UNU(N), N = 1, ..., NU+1 can be used which gives probabilities that each of the N evasions is actually taken. If they are not equally likely, then the "weighted probability of success (WTPAVG) against an alerted submarine" is computed. The equation for WTPAVG is

$$\text{WTPAVG} = \frac{\sum_{N=1}^{NU+1} (\text{PPK}(N) \times \text{UNU}(N))}{(NU+1)} \quad (33)$$

The results of the mathematical development have produced methods of computing the probability of success (PAVG) for an alerted submarine

with equally likely evasion turns, the probability of success (WTPAVG) for an alerted submarine with evasion turns that are not equally likely, and finally the probability of success (PROB) for an unalerted submarine. These probabilities are used to analyze and compare ASW vehicles.

3. Input Data Rules.

A complete run for the computer program (Appendix C) consists of 25 input cards. Each input data card represents the value of one variable except for the last two cards, one of which contains the values for the $AA(i)$, $i=1, \dots, 5$ and the other which contains the $UNU(N)$ values, $N=1, \dots, NU+1$.

One of the first functions of the program is to set the indices $NO=1$ and $M=1$. (See Appendix B--Flow Charts.) The index NO is used to number the pages of the program output. The index M is compared with $NEXT$ (initially set equal to one). The comparison dictates whether the program will continue or terminate. The value for $NEXT$ determines the number of runs to be executed and is an input to the program. The computer then reads the input data cards from SUBROUTINE INPUT after which the 25 values are printed on page 1 of the output. The index NO is increased by one. The programmed computations are performed and the results are printed on page 2 of the output (Figure 6). The indices NO and M are then increased by one. The index M is compared to $NEXT$ and if $NEXT$ is greater than M , SUBROUTINE INPUT searches for more input data cards. Since the program is used to compare and evaluate systems, only a few variables will be changed for each successive run. However, more or all the variables can be changed as long as the input procedure is followed. For example, to compare the three vehicles in Table 1, first place the parameters for the High Speed Surface Vehicle, $RAI = 5.0$, and a value for $NEXT$ in the data input for Run 1. (See Figure 4.) The next run consists of a Locator Card which initiates the reading of Variable Change Card, which in turn changes the value of RAI to 10. The subsequent

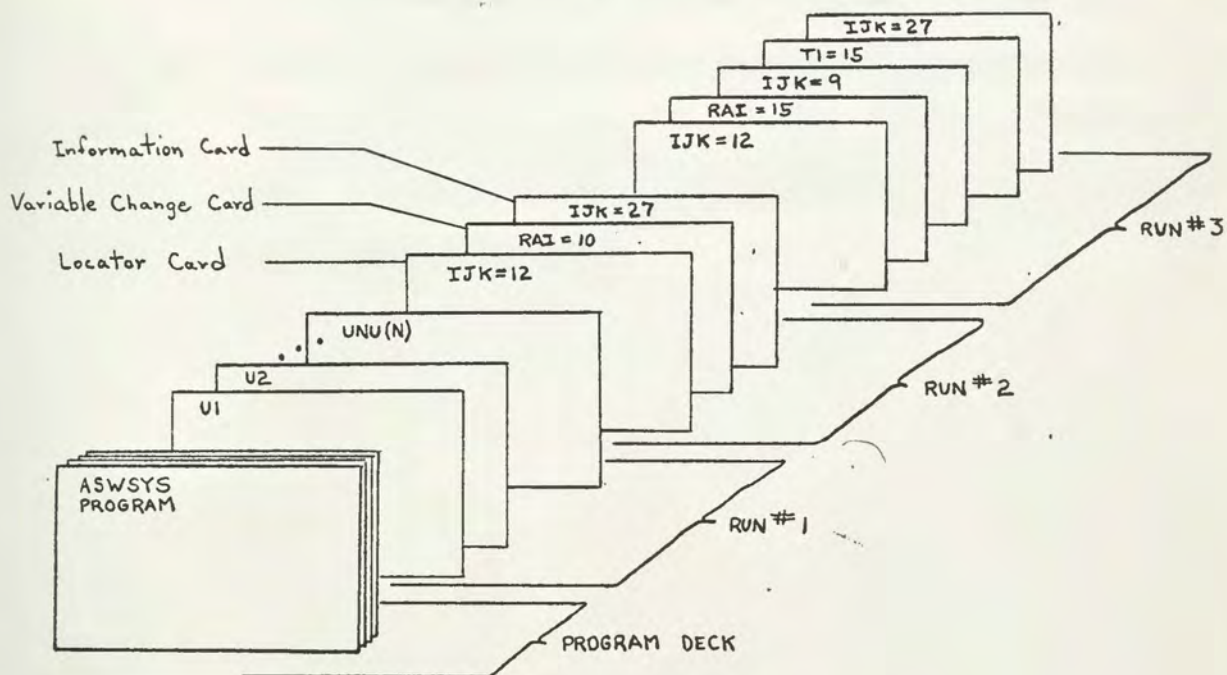


Figure 4 Input Data Procedure

card would be the Information Card, which indicates no further changes for the second run -- start computations. For this run the variable RAI has changed and all other parameter values remain the same.

If another variable change were desired, another Locator Card, Variable Change Card, and Information Card would be placed after the RAI Variable Change Card as indicated in Run 3 in Figure 4.

A run following the initial run takes a minimum of three cards. If only one variable is being changed (e.g. $RAI = 10$), then three cards are necessary. This procedure is followed for $RAI = 5, 10, \dots, 60$ for each system in Table 1 in order to compute probabilities of success for each vehicle over the entire RAI range.

TABLE 1

PARAMETER INPUTS
FOR SAMPLE ASW SYSTEMS

	HIGH SPEED SURFACE VEHICLE		VERTOL VEHICLE		SEAPLANE TYPE VEHICLE
U1	8.0	SLO SUB	18.0	FAST SUB	
U2	3.0		8.0		
U3	15.0		30.0		
Z		45.00		120.00	200.00
PTOT		3.00		4.00	5.00
TOT		.00		1.00	5.00
CLDT		.00		2.00	5.00
RELT		3.00		5.00	5.00
T1		10.00		10.00	10.00
THETA		45.00		45.00	45.00
BETA		10.00		10.00	10.00
TR		4000.00		4000.00	4000.00
PSI		60.00		60.00	60.00
DELTAL		330.00		330.00	330.00
BRGER		1.00		2.00	.50
EXPRNG		3.00		5.00	6.00
PRCNTN		4.00		2.00	4.00
PRCNTS		5.00		5.00	5.00
THDEL		5.00		5.00	5.00
UERR		5.00		2.00	5.00
NU		6		6	6
AA(I)	-1.28	-.52	.00	.52	1.28
UNU(N)	.10 , .05	.00	.10	.40	.30 , .05
					(SAME FOR 3 SYSTEMS)
					(SAME FOR 3 SYSTEMS)

4. An Example and Some Applications.

The simulation possesses the capability of being used as a tool to analyze and compare ASW vehicles as explained in the previous sections. In order to illustrate this capability, the parameters listed for each system in Table 1, and ranges RAI=5, 10, 15, ..., 60 nautical miles were used as input data in the computer program (Appendix B) and processed in the CDC-1604 computer. The program is written in FORTRAN-60. The flow chart is illustrated in Appendix C.

A sample output for the Seaplane Type Vehicle using the parameters of Table 1 and RAI=45 is shown in Figures 5 and 6. The former is a list of all the parameter values for the indicated run. This list enables one to insure that the correct parameters for that run are being properly read into the computer. The latter page contains the probabilities of success for one run. The probabilities for each RAI are plotted on graphs. Each vehicle is depicted on an individual graph. Each graph has six curves -- three drawn from values calculated from using a slow submarine as an adversary and three drawn from using a fast submarine as an adversary (see Figures 7, 8, 9).

The parameter values in this sample are strictly hypothetical and demonstrate only the use of the simulation. However, with these chosen parameter values it can be seen in Figures 7, 8, and 9 that throughout the range of RAI the High Speed Surface Vehicle has probabilities of success considerably lower than the other systems. The slower the speed of the vehicle, the lower the probability because of a low closing rate and long blind time. The probabilities of success are higher at shorter RAI for the VERTOL Vehicle as compared with the Seaplane-Type Vehicle,

COMPLETE INPUT PARAMETER SET

PARAMETER	VALUE	MEANING
U1	8.00	SUBMARINE CRUISE SPEED (KNOTS)
U2	3.00	SUBMARINE SILENT SPEED (KNOTS)
U3	15.00	SUBMARINE FAST SPEED (KNOTS)
Z	200.00	VEHICLE TRANSIT SPEED TO DATUM (NEGLECT ACCEL. OR DECEL.)
PTOT	5.00	PRE TAKE OFF TIME (MIN)
TOT	5.00	TAKE OFF TIME (MIN)
CLDT	5.00	LAND TIME (MIN)
RELT	5.00	TARGET RELOCATION TIME (MIN)
T1	10.00	ELAPSED TIME OF SUB AT SPEED U3 (MIN)
THETA	45.00	COURSE OF SUB AT LAST KNOWN POSITION (DEGREES)
BETA	10.00	TRUE BEARING OF SUB FROM VEHICLE (DEGREES)
RAI	45.00	RANGE TO SUB AT LAST KNOWN POSITION FROM VEHICLE (MILES)
TR	4000.00	TURNING RADIUS OF SUB (YDS)
PRCNTN	4.00	NAV. ERROR IN PERCENT DISTANCE TO SUB
PRCNTS	5.00	SENSOR RANGE ERROR IN PERCENT SENSOR RANGE
BRGER	.50	SENSOR BEARING ERROR IN DEGREES
EXPRNG	6.00	RANGE EXPECTED FROM SENSOR FOR LOCALIZATION AT DATUM, MILES
PSI	60.00	LEFT BOUND FOR SUB EVASIVE TURN IN DEGREES
DELTA	330.00	RIGHT BOUND FOR SUB EVASIVE TURN IN DEGREES
NU	6	NUMBER OF INCREMENTS CONSIDERED IN PSI-DELTA RANGE
NEXT	24	NUMBER OF SETS OF INPUT DATA
UERR	5.00	SUBMARINE SPEED ERROR (KNOTS)
THDEL	5.00	SUBMARINE COURSE ERROR (DEGREES)

FIGURE 5

INPUT PARAMETERS

VEHICLE SPEED (KNOTS)	PRE TAKE OFF TIME (MIN)	TAKE OFF TIME (MIN)	LAND TIME (MIN)	TARGET RELOCATION TIME (MIN)	SUBMARINE CRUISE SPEED (KNOTS)	SUBMARINE SILENT SPEED (KNOTS)	SUBMARINE FAST SPEED (KNOTS)
200.00	5.00	5.00	5.00	5.00	8.00	3.00	15.00

SUBMARINE TO VEHICLE RANGE (MILES)	SUBMARINE COURSE (DEGREES)	TRUE BEARING SUB FROM VEHICLE (DEGREES)	NAVIGATION ERROR (PERCENT) DISTANCE)	SENSOR RANGE ERROR (PERCENT) RANGE)	SENSOR BEARING ERROR (DEGREES)	EXPECTED RANGE OF LOCALIZATION SENSOR (MILES)
45.00	45.00	10.00	4.00	5.00	.50	6.00

AVERAGE SUCCESS PROBABILITY FOR 7 EVASION TACTICS IS .539
 AVERAGE WEIGHTED SUCCESS PROBABILITY FOR 7 EVASION TACTICS IS .073
 AVERAGE SUCCESS PROBABILITY FOR UNALERTED SUBMARINE IS .679

COMPUTED VALUES FOR SUBMARINE EVASION

EVASIVE NUMBER	EVASION TURN (DEGREES)	SUCCESS PROBABILITY	BLIND TIME (MIN)	DISTANCE TRANSIT TO DATUM (MILES)	RELATIVE SPEED (KNOTS)	SIG TOTAL (MILES)
1	-30.00	.539	33.96	52.18	193.39	2.03
2	-15.00	.621	33.96	52.18	193.39	2.03
3	.00	.656	33.96	52.18	193.39	2.03
4	15.00	.621	33.96	52.18	193.39	2.03
5	30.00	.539	33.96	52.18	193.39	2.03
6	45.00	.441	33.96	52.18	193.39	2.03
7	60.00	.355	33.96	52.18	193.39	2.03

FIGURE 6

HIGH SPEED SURFACE VEHICLE

$V = 45$
 $RT = 6$
 $BRGR = 1.0$
 $PRCMTN = 4.0$
 $EXPNG = 3.0$
 $PRCNTS = 5.0$
 $THDEL = 5.0$
 $VERR = 5.0$

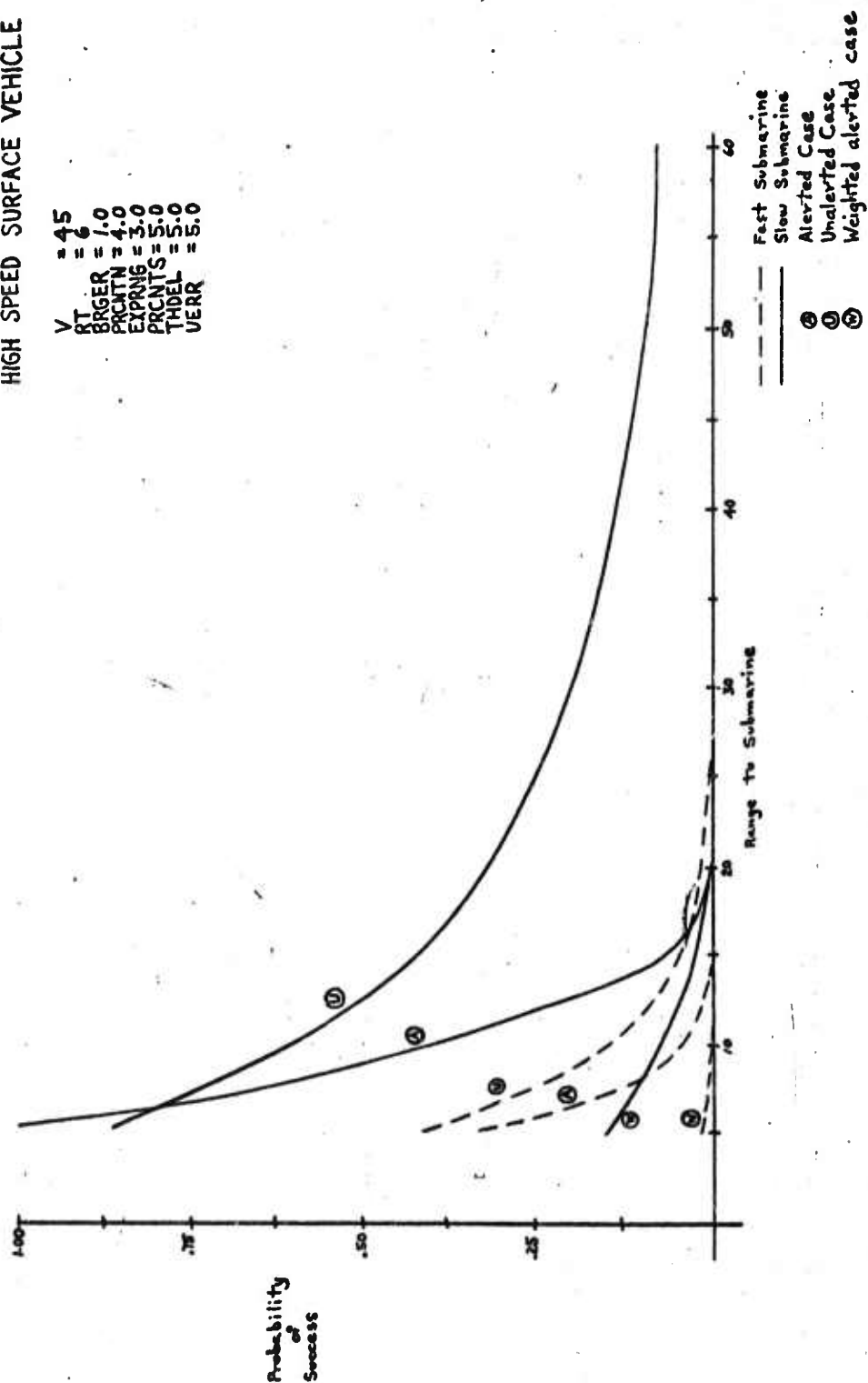


Figure 7

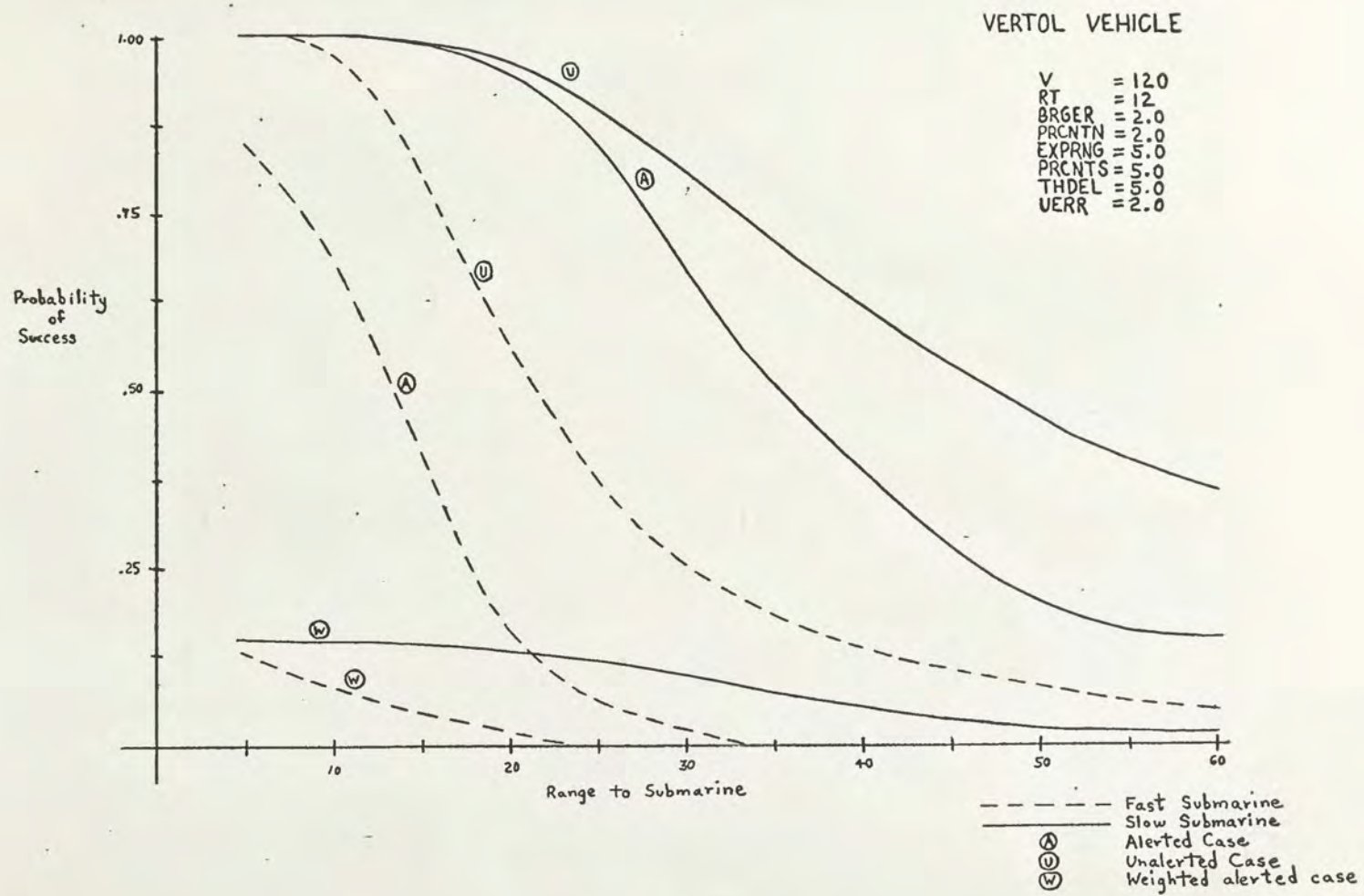


Figure 8

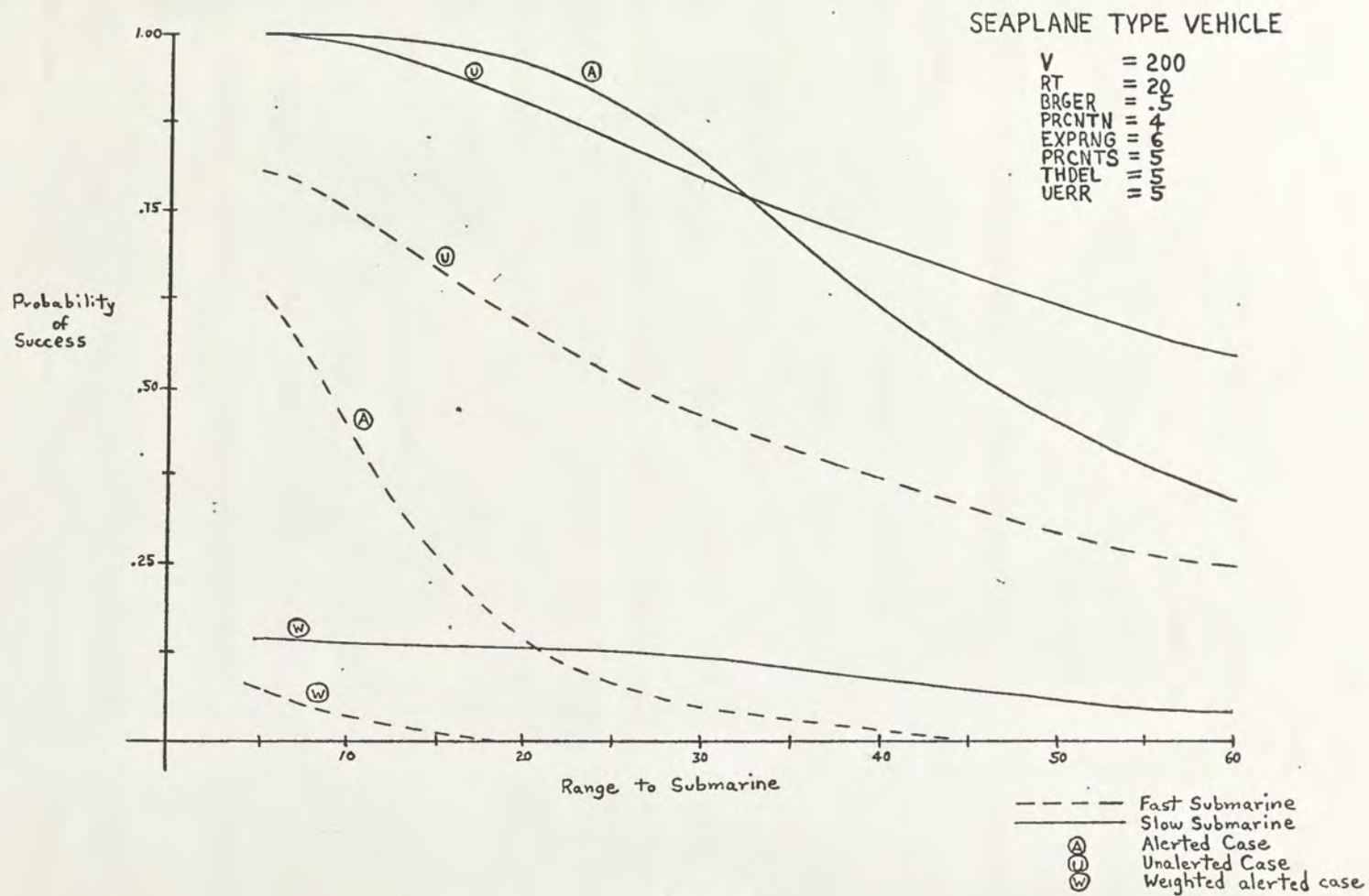


Figure 9

but a crossover point occurs at approximately $RAI=25$, where the Seaplane-Type Vehicle has higher probabilities of success. The crossover is a result of the values selected in the sample for the vehicle speed, reaction time, and expected sonar range. From these results the best vehicle can be chosen and the other vehicles investigated for improvements.

In addition to the example stated above several applications are suggested for the simulation. One application is to use the simulation to determine what parameters or characteristics the vehicle and the sensors must have to obtain a given probability of success. For example, if the state-of-the-art for active sensors dictates that five nautical miles is the maximum range expected for active sensors for the next ten years, then it would be advantageous to find values of vehicle speed, reaction time, navigation errors, and prediction errors that can be tolerated for the vehicle and still maintain a given probability of success. The development of a new ASW vehicle could be directed towards achieving these parameter values.

Another application can be made if a new sensor is being proposed for a given vehicle. The values for the expected active sensor range and the sensor errors can be computed for a given probability of success. These parameter values can be used as design limits in the development of the proposed sensor.

Finally the simulation can be used if intelligence indicated that a new enemy submarine is in existence. The simulation can be used to indicate how well the present vehicles will perform against the new threat relative to the old threat.

5. Conclusions.

The example in Section 4 is the type of comparison that can be performed for various kinds of ASW vehicles. There are several decisions-- evasion tactics used, submarine type used, and so on--that have to be made prior to using the program; but once the decisions are made for a given situation, they have to remain the same for all systems being compared. Several modifications and suggestions for the model are discussed below.

It might be argued that an elliptical coverage function should be used instead of a circular coverage function because of the elliptical sensor locating error. This change can be made by rewriting SUBROUTINE OCIP of the computer program (Appendix C).

Instead of evasion turns limited to 90 degrees either side of the course line, they could be programmed for 360 degrees evasion; i.e., 180 degrees either side of the course line.

It must be realized that the depth of the submarine has no direct influence on this simulation. Therefore, this has to be kept in mind when parameter values such as EXPRNG are put into the simulation. It is possible that EXPRNG could be less in an evasion problem where the submarine is more likely to increase its depth, and therefore, EXPRNG should be reduced.

It would be possible to give the vehicle freedom of movement before transit commences, rather than being motionless. But the advantages of the passive tactic for the vehicle are then relinquished.

The restriction on T1 in the alerted submarine case could be abolished by programming for the possibility of having a speed change executed before a turn is completed.

Possibly a passive sensor detached from the vehicle could transmit current information about the submarine's actions while the vehicle is inbound to intercept the submarine. This would increase the probability of success.

In the foregoing sections, the simulation has been described and the mathematical development shown. In addition, the use of the computer program has been illustrated and an example and its results briefly analyzed. The use of the simulation is simple and the results easily understood. Therefore, it is recommended that the use of this simulation be employed to compare and analyze proposed ASW vehicles and operational ASW vehicles.

BIBLIOGRAPHY

1. Operations Research Incorporated, Silver Spring, Maryland. Use of the Circular Coverage Function in Calculation of A/S Kill Probabilities, by G. B. Yntema, H. D. Kushner, and R. A. Gibbons. August 26, 1958. Prepared under Navy Bureau of Ordnance, Contract NOrd 17976.
2. Parzen, E., Modern Probability Theory and Its Applications. John Wiley & Sons, Inc., 1960.
3. Operations Evaluation Group, Washington, D. C., Model and Computer Program for an Attack on an Evading Submarine, by S. H. Howe, J. F. Hammerle, and R. D. Mason, Jr., June 8, 1962. IRM-18.
4. RAND. Circular Coverage Function, by H. H. Germand. January 26, 1950. RM-330.

APPENDIX A

GLOSSARY

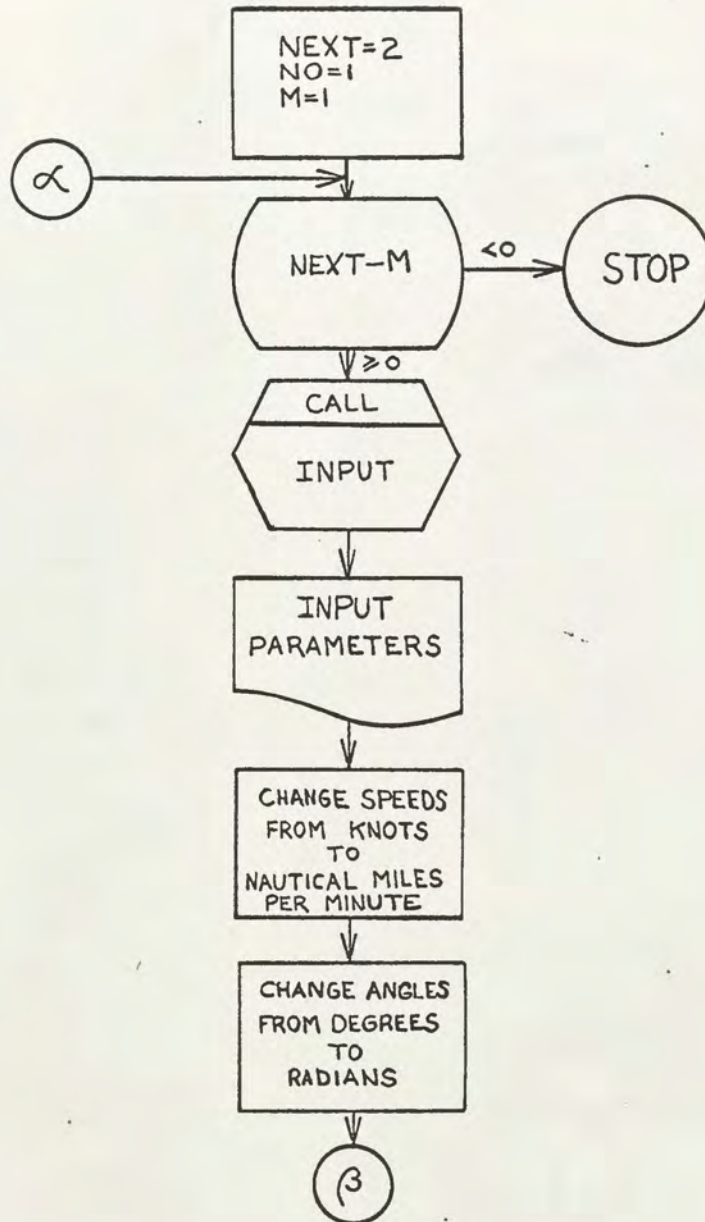
Notation	Meaning
A(1),...,A(5)	- Number of standard deviations from the mean of the normal density function. Each A(i) is the midpoint of a segment of area which represents 20% of the total area under the normal density function. The A(i)'s are used in the prediction error of the unalerted submarine case.
AB	- Evasion turn in degrees from the estimated submarine course.
BETA	- True bearing of the submarine from the vehicle (degrees).
BIAS(N)	- Distance from EP to the terminal point of the N th evasion.
BRGER	- Sensor bearing error in degrees.
CLDT	- Land time (min.) which includes time to land into the wind and taxi time to get into position to employ active sensors.
DELTA	- Bound to the right of the known submarine course. This bounds to the right the set of possible evasion turns (degrees).
DIST	- Distance the submarine travels during blind time, assuming a constant course and speed.
EP	- Estimate position of the submarine after blind time has expired.
EXPRNG	- Expected range of the active sensor used by the vehicle in re-establishing contact at the EP (in nautical miles).
NEXT	- Number of data runs for the computer program.
NU	- Number of increments considered with the (PSI-DELTA) range of the set of possible turns.
PAVG	- Average probability of success for N evasions considered in the alerted submarine case.
PRCNTN	- Navigation error in percent of distance traveled.

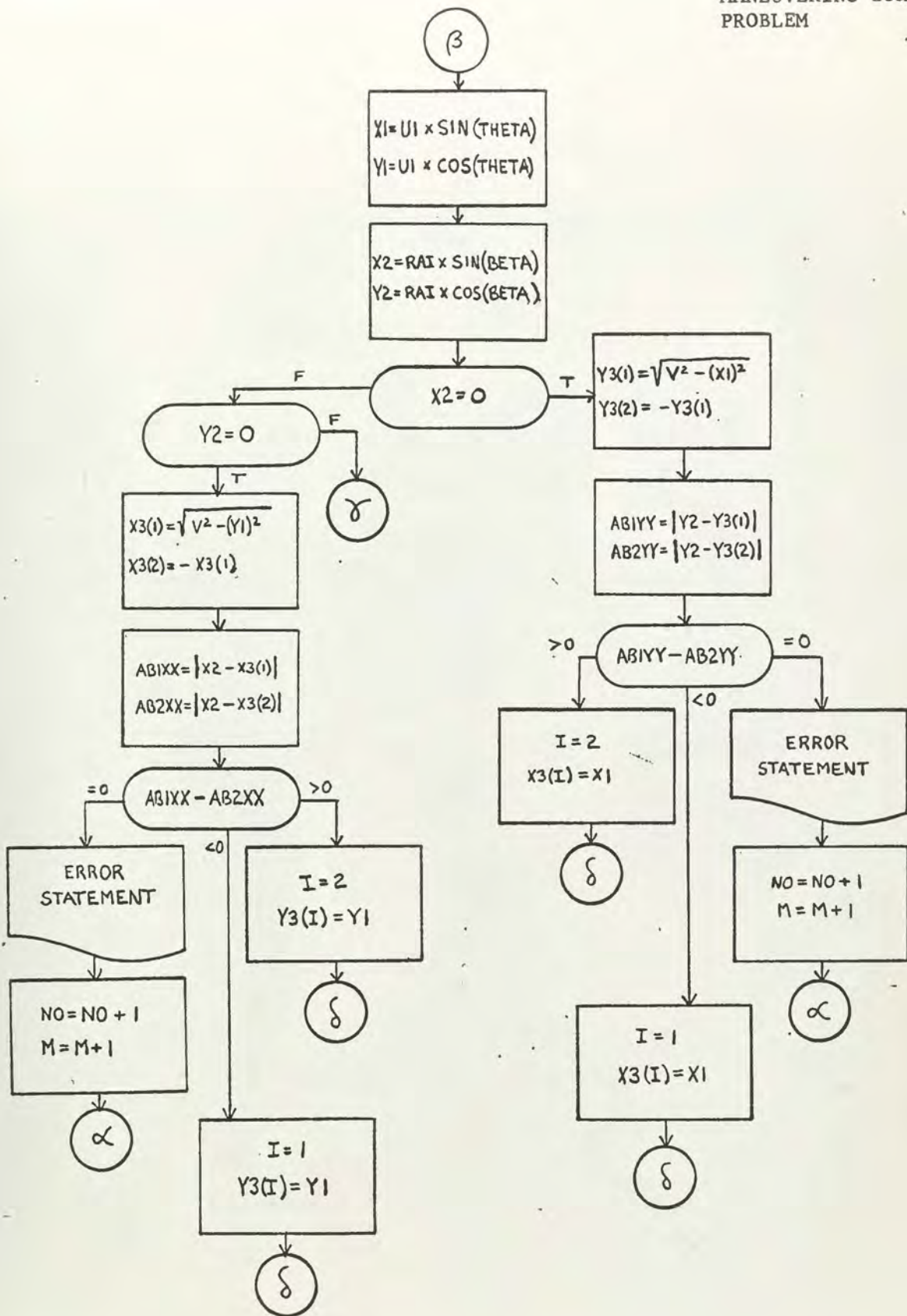
Notation	Meaning
PRCNTS	- Sensor range error in percent of sensor range.
PROB	- Probability of success for the unalerted submarine case.
PSI	- Bound to the left of the last known submarine course. This bounds to the left the set of possible evasion turns (degrees).
PTOT	- Pre take-off time (min.) which commences when the vehicle can no longer observe the submarine and includes decision time, warm-up time, and sensor retrieval time.
RAI	- Range from the vehicle to the submarine at the last known position (nautical miles).
RELT	- Target relocation time (min) which includes the time to deploy sensors and ends when the submarine is relocated.
RT	- Reaction time which is the sum of PTOT, TOT, CLDT, and RELT.
SBIAS(I,J)	- Distance between the (i,j) th cell and EP.
SIGJT	- Total standard deviation of errors.
TB	- Blind time which is the sum of the reaction time (RT) and the transit time (TD).
TD	- Time it takes the vehicle to travel from its initial position to EP.
Tl	- Tactical interval of time (min.) after evasion commences during which the submarine travels at fast speed. After Tl has elapsed, the submarine slows to silent speed.
THDEL	- Submarine course error (degrees).
THETA	- Course of the submarine (degrees) at the last known position.
TOT	- Take-off time (min.) which includes take-off roll and the time to maneuver into the wind.
TR	- Turning radius of the submarine.

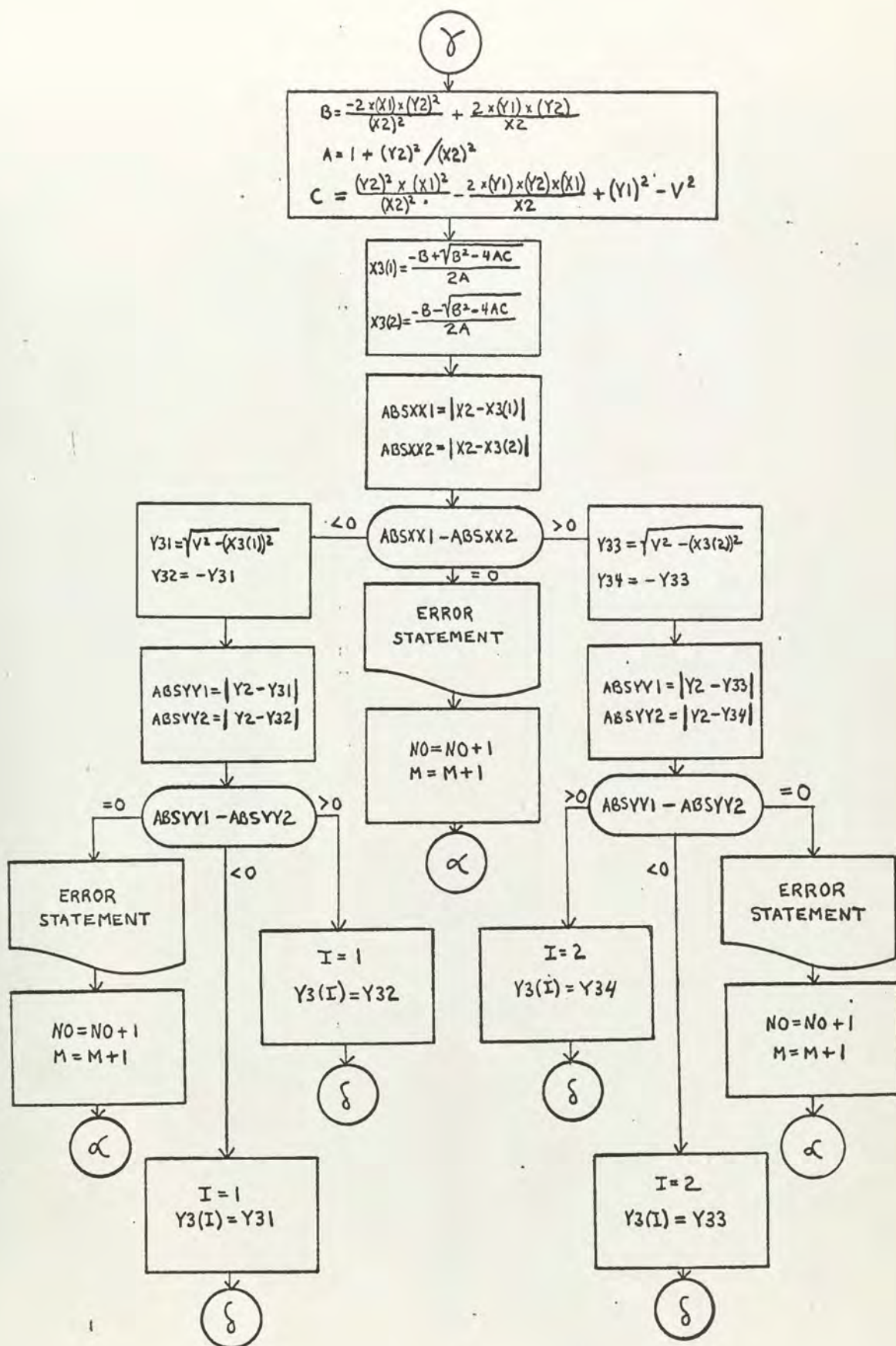
Notation	Meaning
UERR	- Submarine speed error (knots).
UNU(1),...,UNU(NU+1)	- The set of probabilities for $N=1, \dots, NU+1$ evasion turns. These are used when evasion turns considered are not equally likely.
U1	- Submarine cruise speed (knots).
U2	- Submarine silent speed (knots).
U3	- Submarine fast speed (knots).
V	- Average vehicle transit speed (knots)
WTPAVG	- Weighted probability of success for the alerted submarine case.
(X2,Y2)	- Last known position of the submarine.
(X(N),Y(N))	- Terminal point of the N^{th} evasion after blind time has expired.
Z	- Average vehicle transit speed (knots). Neglect acceleration and deceleration time.

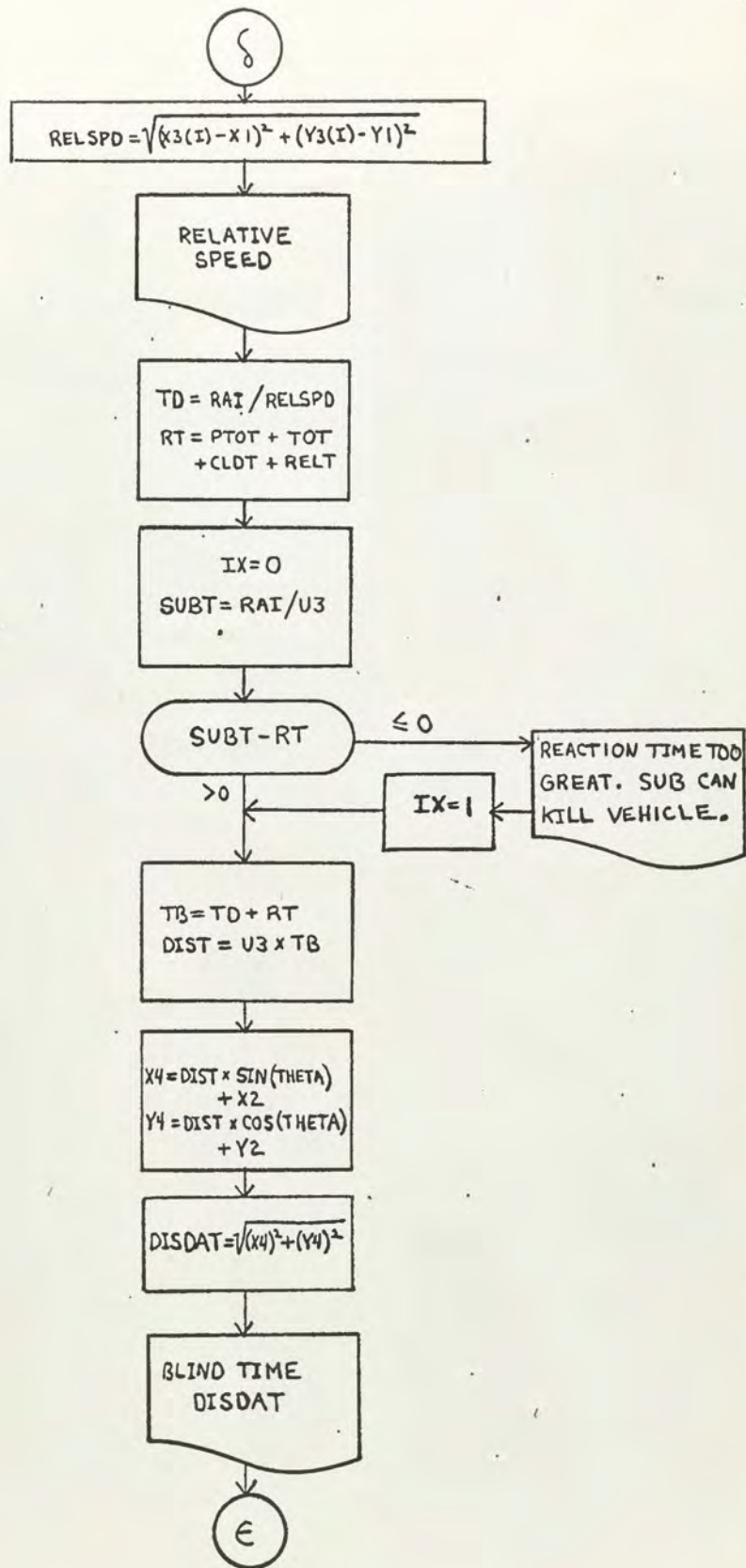
APPENDIX B

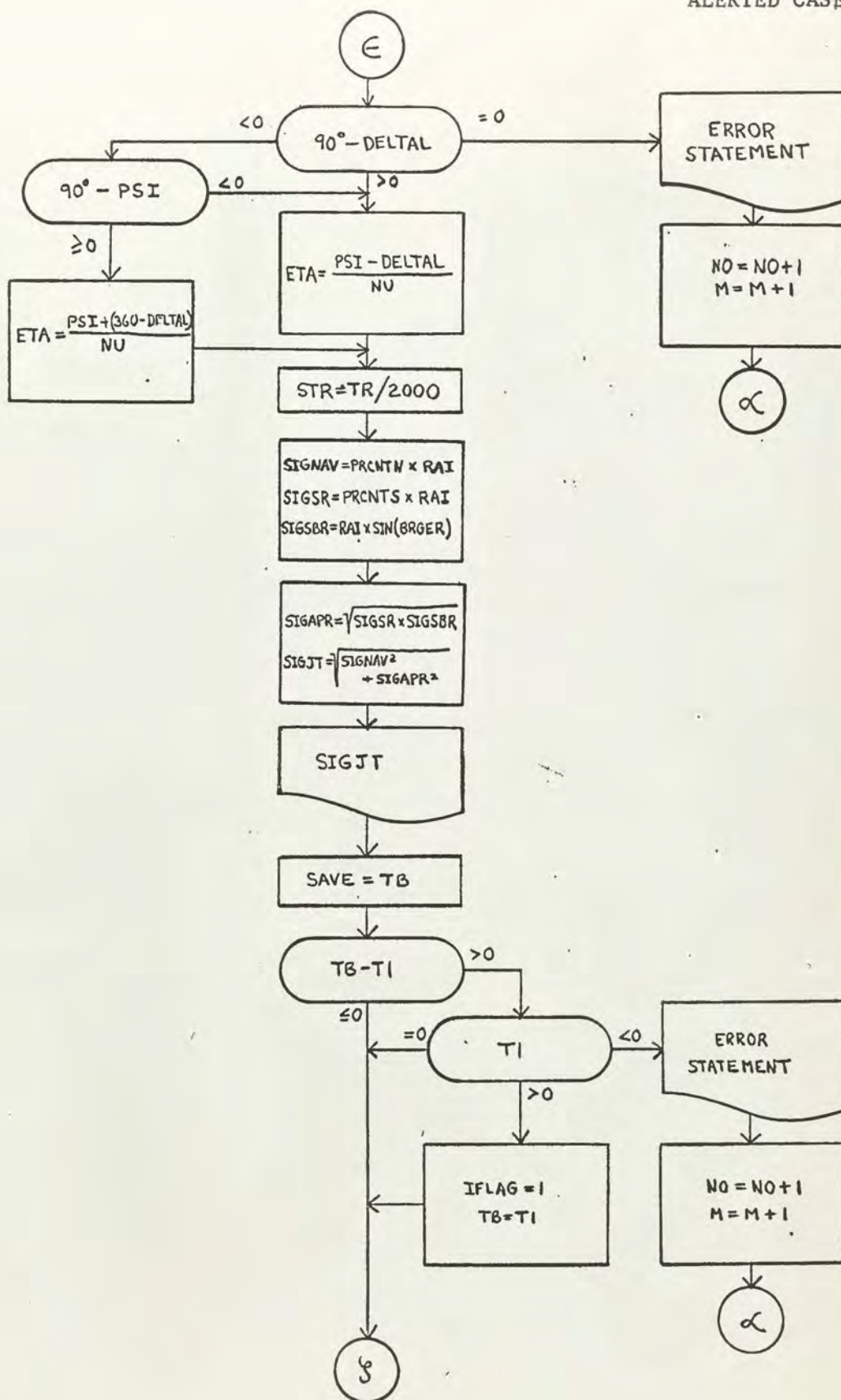
INPUT AND UNIT CHANGES

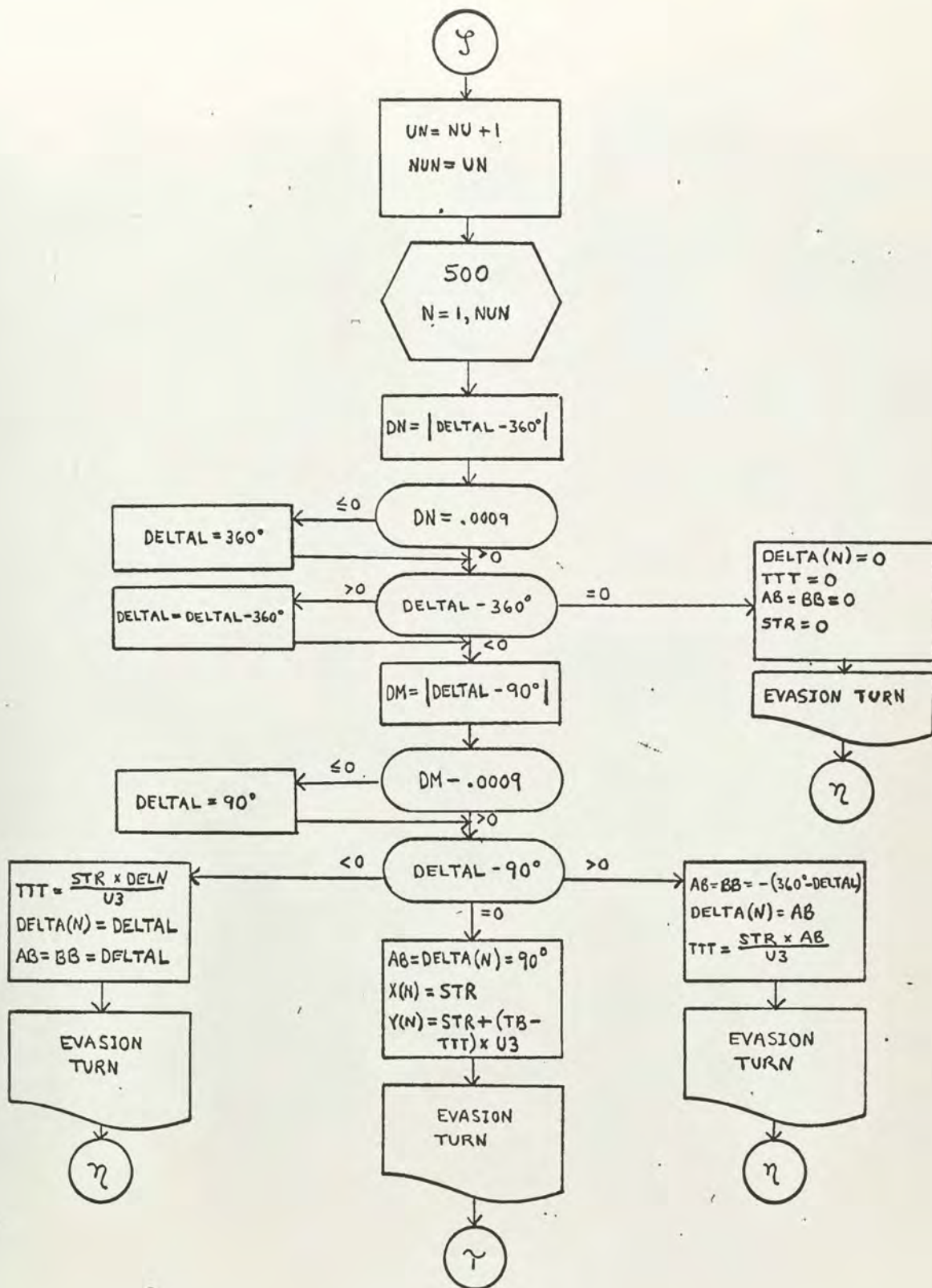


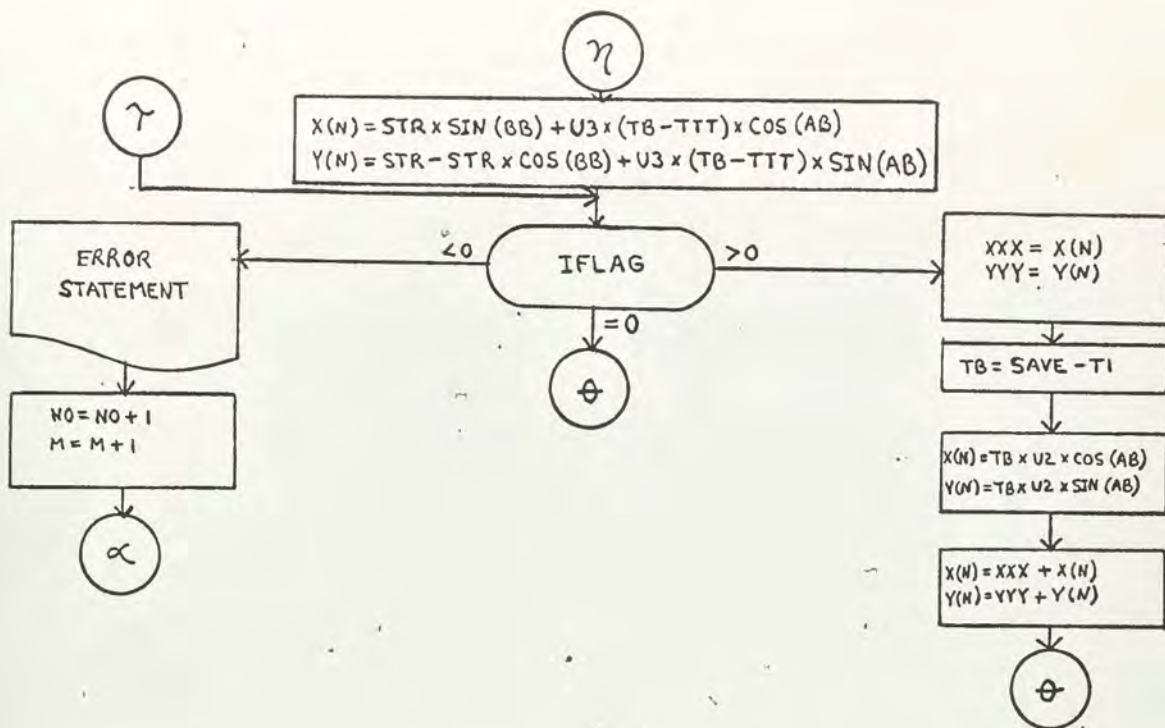




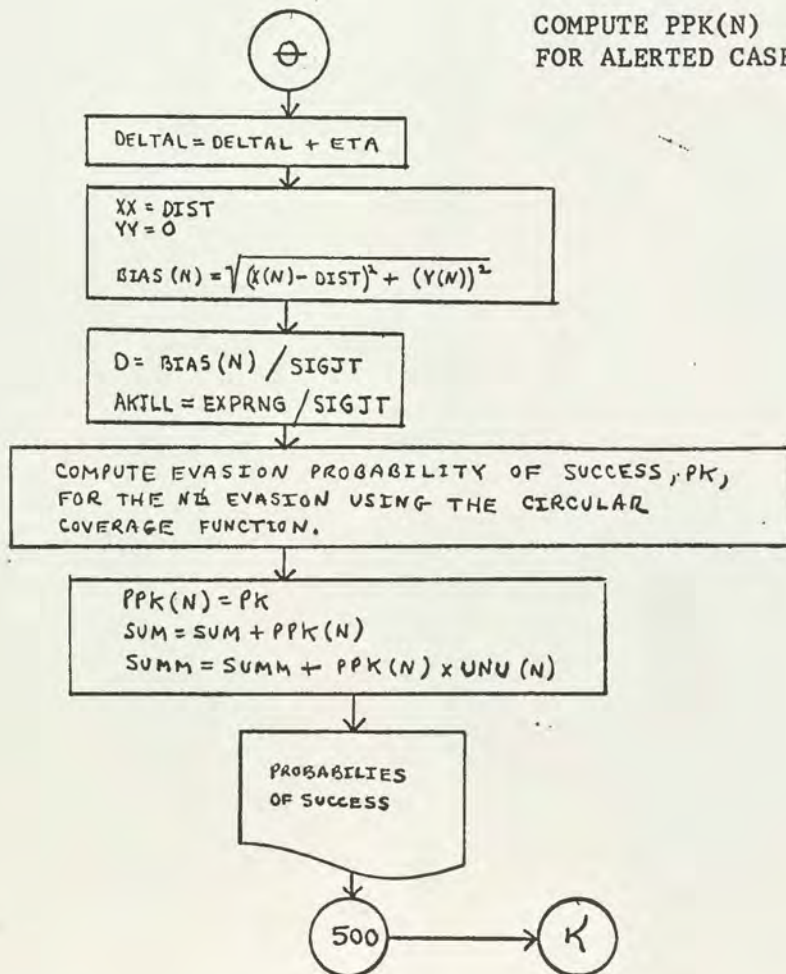


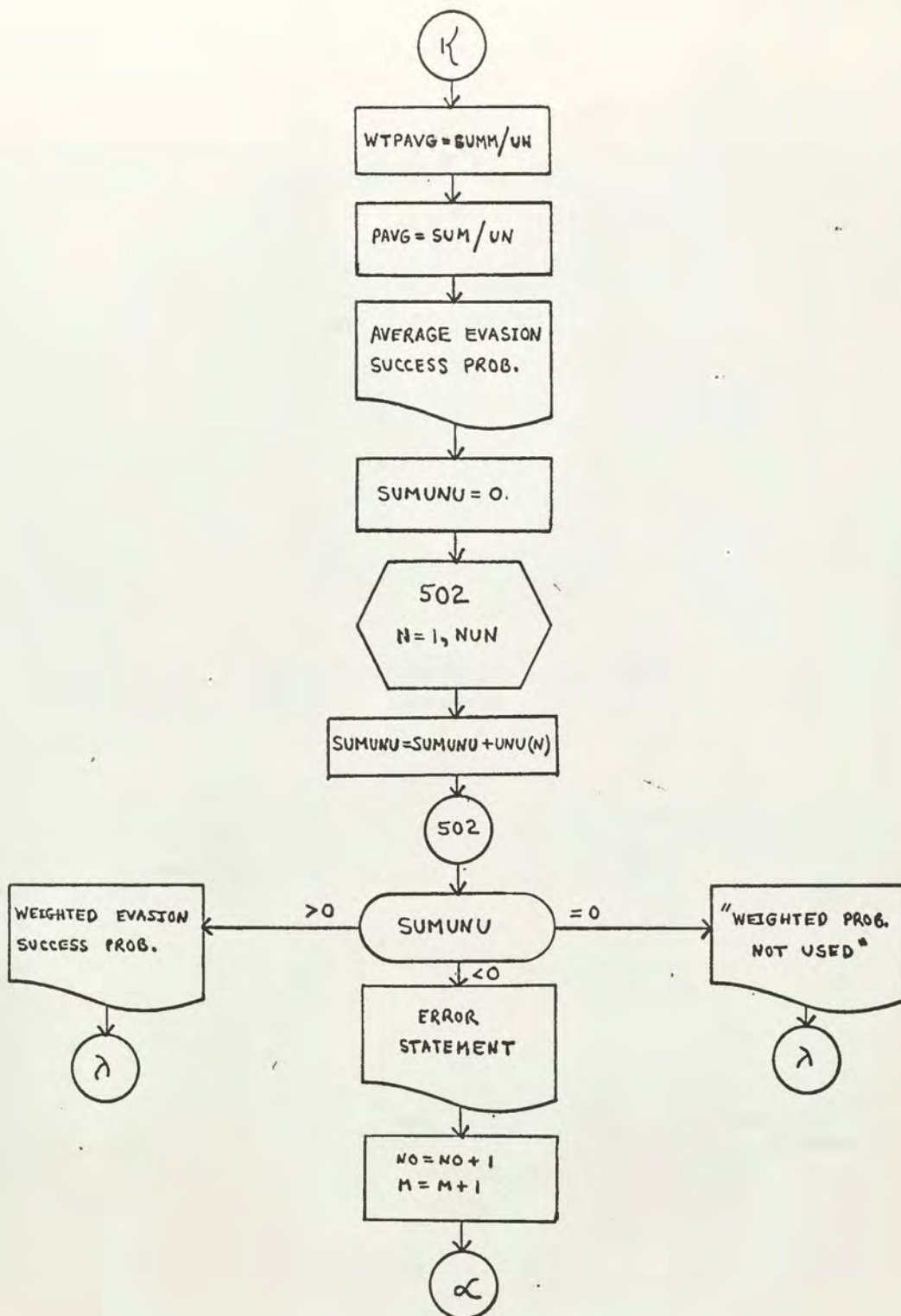


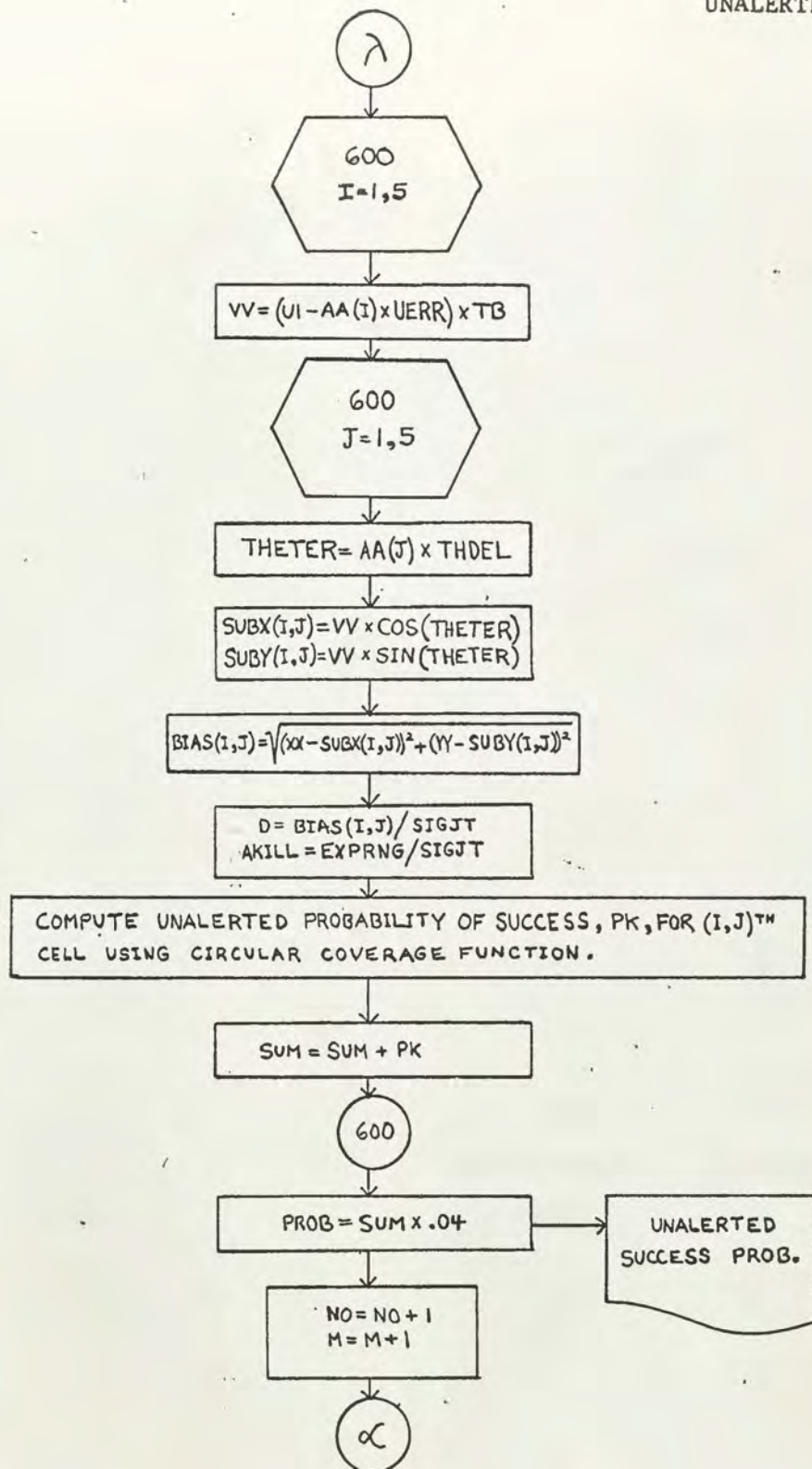




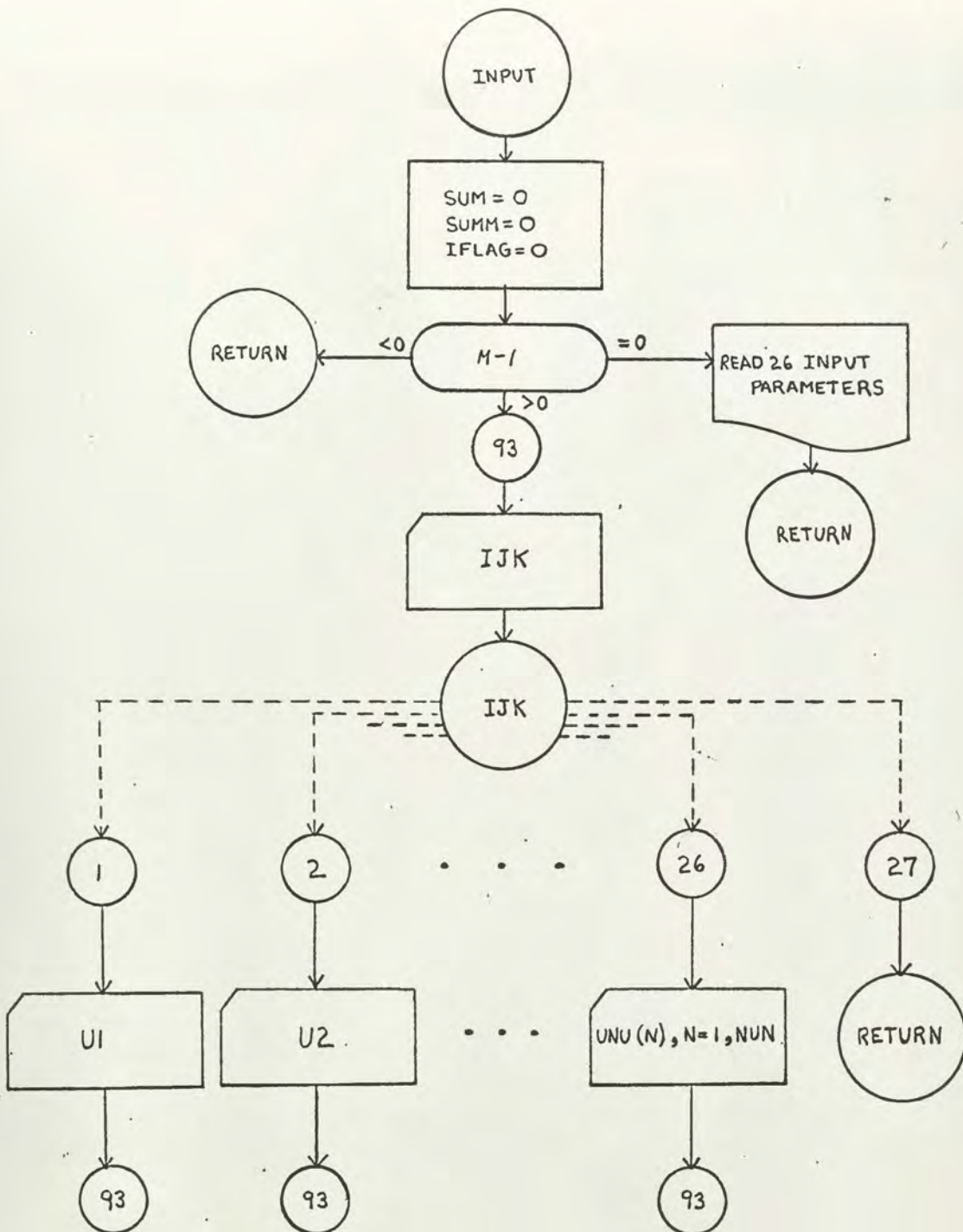
COMPUTE PPK(N)
FOR ALERTED CASE







SUBROUTINE INPUT



C	PROGRAM ASWSYS	0010
C	THE PROGRAM COMPUTES PROBABILITIES OF AN ASW VEHICLE VS. AN	0020
C	EVASIVE SUBMARINE AS A FUNCTION OF REACTION OF THE VEHICLE.	0030
	DIMENSION Y3(2),X3(2),DELTA(30),X(30),Y(30),BIAS(30),AA(5),	0040
	1SUBX(5,5),SUBY(5,5),SBIAS(5,5),PPK(15),UNU(15),ZZ(4)	0050
	NEXT=2	0060
	NO=1	0070
	M=1	0080
20	IF(NEXT-M)9000,30,30	0090
30	CALL INPUT(U1,U2,U3,Z,PTOT,TOT,CLDT,RELT,T1,THETA,BETA,RAI,TR,	0100
	1PRCNTN,PRCNTS,BRGER,EXPRNG,PSI,UERR,THDEL,NU,NEXT,DELTAL,SUM,AA,IF	0110
	2LAG,UNU,DELN,SUM,M)	0120
C	OUTPUT ALL INPUTS.	0130
	GO TO 1999	0140
C	CONVERT KNOTS TO MILES PER MINUTE, AND DEGREES TO RADIANS	0150
40	SV=Z*.01667	0160
	SU1=U1*.01667	0170
	SU2=U2*.01667	0180
	SU3=U3*.01667	0190
	SUERR=UERR*.01667	0200
	STHETA=THETA/57.29578	0210
	SBETA=BETA/57.29578	0220
	SPSI=PSI/57.29578	0230
	SDELTA=DELTAL/57.29578	0240
	SBRGER=BRGER/57.29578	0250
	STHDEL=THDEL/57.29578	0260
C	SET UP MANEUVERING BOARD SOLUTION TO SOLVE FOR THE POSITION THE	0270
C	SUBMARINE WILL BE WHEN THE VEHICLE INTERCEPTS IT, ASSUMING A	0280
C	CONSTANT COURSE/SPEED FOR THE SUBMARINE.	0290
	X1=SU1*SINF(STHETA)	0300
	Y1=SU1*COSF(STHETA)	0310
C	(X1,Y1) AND (0,0) ARE TWO POINTS THAT INDICATE THE CUS/SPD OF THE	0320
C	SUBMARINE.	0330
	X2=RAI*SINF(SBETA)	0340
	Y2=RAI*COSF(SBETA)	0350
C	(X2,Y2) IS THE LAST KNOWN POSITION OF THE SUBMARINE RELATIVE TO	0360
C	VEHICLE AT (0,0). NOW CHECK SPECIAL CASES.	0370
C	THE FOLLOWING 13 STATEMENTS ARE USED TO ROUND OFF X1,X2,Y1,Y2 TO	0380
C	ZERO IF THEY ARE WITHIN + OR - .001 OF ZERO.	0390
	ZZ(1)=X1	0400
	ZZ(2)=Y1	0410
	ZZ(3)=X2	0420
	ZZ(4)=Y2	0430
	DO 52 I=1,4	0440
	ABZZ=ABSF(ZZ(I))	0450
	IF(ABZZ-.001)51,51,52	0460
51	ZZ(I)=0.	0470
52	CONTINUE	0480

X1=ZZ(1)
 Y1=ZZ(2)
 X2=ZZ(3)
 Y2=ZZ(4)
 IF(X2)105,100,105
 100 Y3(1)=SQRTF(SV**2-X1**2)
 Y3(2)=-SQRTF(SV**2-X1**2)
 Y3A=Y3(1)
 Y3B=Y3(2)
 AB1YY=ABSF(Y2-Y3A)
 AB2YY=ABSF(Y2-Y3B)
 IF(AB1YY-AB2YY)102,9050,103
 102 I=1
 GO TO 104
 103 I=2
 104 X3(1)=X1
 GO TO 200
 105 IF(Y2)110,106,110
 106 X3(1)=SQRTF(SV**2-Y1**2)
 X3(2)=-X3(1)
 X3A=X3(1)
 X3B=X3(2)
 AB1XX=ABSF(X2-X3A)
 AB2XX=ABSF(X2-X3B)
 IF(AB1XX-AB2XX)107,9050,108
 107 I=1
 GO TO 109
 108 I=2
 109 Y3(I)=Y1
 GO TO 200
 110 B=(-2.*X1*Y2*Y2)/(X2**2)+((2.*Y1*Y2)/X2)
 A=1.+(Y2**2/X2**2)
 C=((Y2**2*X1**2)/X2**2)-(2.*Y1*Y2*X1)/X2+Y1**2-SV**2
 X3(1)=(-B+SQRTF(B**2-4.*A*C))/(2.*A)
 X3(2)=(-B-SQRTF(B**2-4.*A*C))/(2.*A)
 X3A=X3(1)
 X3B=X3(2)
 ABSXX1=ABSF(X2-X3A)
 ABSXX2=ABSF(X2-X3B)
 IF(ABSXX1-ABSXX2)125,9050,155
 125 I=1
 Y31=SQRTF(SV**2-X3A**2)
 Y32=-Y31
 ABSYY1=ABSF(Y2-Y31)
 ABSYY2=ABSF(Y2-Y32)
 IF(ABSYY1-ABSYY2)130,9050,135
 130 I=1
 Y3(I)=Y31

0490
 0500
 0510
 0520
 0530
 0540
 0550
 0560
 0570
 0580
 0590
 0600
 0610
 0620
 0630
 0640
 0650
 0660
 0670
 0680
 0690
 0700
 0710
 0720
 0730
 0740
 0750
 0760
 0770
 0780
 0790
 0800
 0810
 0820
 0830
 0840
 0850
 0860
 0870
 0880
 0890
 0900
 0910
 0920
 0930
 0940
 0950
 0960

	GO TO 200	097C
135	I=1	098C
	Y3(I)=Y32	099C
	GO TO 200	100C
155	I=2	101C
	Y33=SQRTF(SV**2-X3B**2)	102C
	Y34=-Y33	103C
	ABSY1=ABSF(Y2-Y33)	104C
	ABSY2=ABSF(Y2-Y34)	105C
	IF(ABSY1-ABSY2)140,9050,150	106C
140	I=2	107C
	Y3(I)=Y33	108C
	GO TO 200	109C
150	I=2	110C
	Y3(I)=Y34	111C
200	X3II=X3(I)	112C
	Y3II=Y3(I)	113C
	RELSPD=SQRTF((X3II-X1)**2+(Y3II-Y1)**2)	114C
	RSPD=RELSPD/.01667	115C
C	COMPUTE FLYING TIME TO DATUM	116C
	TD=RAI/RELSPD	117C
C	COMPUTE REACTION TIME	118C
	RT=PTOT+TOT+CLCT+RELT	119C
	IX=0	120C
	SUBT=RAI/SU3	121C
	IF(SUBT-RT)202,202,201	122C
202	IX=1	123C
201	CONTINUE	124C
C	COMPUTE OVER ALL REACTION TIME (CALLED BLIND TIME).	125C
	TB=TD+RT	126C
C	COMPUTE DISTANCE TRAVELED BY SUBMARINE DURING BLIND TIME.	127C
	DIST=SU3*TB	128C
C	(X4,Y4)=PREDICTED DATUM POSITION OF SUBMARINE RELATIVE TO VEHICLE	129C
C	AT(0,C).	130C
	X4=DIST*SINF(STHETA)+X2	131C
	Y4=DIST*COSF(STHETA)+Y2	132C
C	DISTANCE FLOWN TO DATUM.	133C
	DISDAT=SQRTF(X4**2+Y4**2)	134C
C	COMPUTE PROBABILITIES FOR ALERTED SUBMARINE EVADING. PLACE SUB IN	135C
C	(0,0) POSITION HEADING 000. RANGE OF SUB EVASION IS FROM DELTA	136C
C	DEGREES TO RIGHT OF 000 TO PSI DEGREES TO THE LEFT WITH INCREMENTS	137C
C	OF ETA DEGREES. FOR COMPUTING PURPOSES 000 IS LAST KNOWN SUB CUS.	138C
	RNU=NU	139C
	IF(1.5708-SDELTA)204,9050,210	140C
204	IF(1.5708-SPSI)210,205,205	141C
205	ETA=(SPSI+(6.28319-SDELTA))/RNU	142C
	GO TO 212	143C
210	ETA=(SPSI-SDELTA)/RNU	144C

```

212 STR=TR/2000.
    SAVE1=STR
C   COMPUTE ERRORS
    SIGNAV=.01*PRCNTN*RA1
    SIGSR=.01*PRCNTS*RA1
    SIGSBR=RA1*SINF(SBRGR)
    SIGAPR=SQRTF(SIGSR*SIGSBR)
    SIGJT= SQRTF(SIGNAV**2+SIGAPR**2)
    SAVE=TB
    IF(TB-T1)299,299,405
405 IF(T1)9050,299,407
407 IFLAG=1
    TB=T1
299 UN=NU+1
    NUN=UN
    DO 50C N=1,NUN
    IF(N-1)9050,301,310
301 DELN=SDELTA
310 DN=ABSF(DELN-6.2832)
    IF(DN-.0009)312,312,314
312 DELN=6.2832
314 IF(DELN-6.2832)300,315,666
315 CONTINUE
    DELTA(N)=0.
    TTT=0.
    AB=0.
    STR=0.
    BB=0.
    GO TO 350
666 DELN=DELN-6.2832
300 CM=ABSF(DELN-1.5708)
    IF(CM-.0009)313,313,316
313 DELN=1.5708
316 IF(DELN-1.5708)320,330,340
320 TTT=STR*DELN/SU3
    AB=DELN
    DELTA(N)=DELN*57.29578
    BB=AB
    GO TO 350
330 AB=1.5708
    DELTA(N)=90.
    X(N)=STR
    Y(N)=STR+(TB-TTT)*SU3
    GO TO 409
340 AB=-(6.2832-DELN)
    DELTA(N)=-(6.2832-DELN)*57.29578
    TTT=STR*AB/SU3
    BB=AB

```

```

1450
1460
1470
1480
1490
1500
1510
1520
1530
1540
1550
1560
1570
1580
1590
1600
1610
1620
1630
1640
1650
1660
1670
1680
1690
1700
1710
1720
1730
1740
1750
1760
1770
1780
1790
1800
1810
1820
1830
1840
1850
1860
1870
1880
1890
1900
1910
1920

```


	STR=-STR	1930
	TTT=-TTT	1940
350	X(N)=STR*SINF(BB)+SU3*(TB-TTT)*COSF(AB)	1950
	Y(N)=STR-STR*CCSF(BB)+SU3*(TB-TTT)*SINF(AB)	1960
400	IF(IFLAG)9050,400,410	1970
410	XXX=X(N)	1980
	YYY=Y(N)	1990
	TB=SAVE-T1	2000
	X(N)=TB*SU2*COSF(AB)	2010
	Y(N)=TB*SU2*SINF(AB)	2020
	X(N)=XXX+X(N)	2030
	Y(N)=YYY+Y(N)	2040
400	DELN=DELN+ETA	2050
	XX=DI ST	2060
	YY=0.	2070
C	COMPUTE BIAS FOR EACH (X(N),Y(N)) RELATIVE TO (XX,YY).	2080
	XNX=X(N)	2090
	YNY=Y(N)	2100
	BIAS(N)=SQRT(((XNX-XX)**2+(YNY-YY)**2)	2110
	D=BIAS(N)/SIGJT	2120
	AKILL=EXPRNG/SIGJT	2130
	STR=SAVE1	2140
	TB=T1	2150
C	COMPUTE PROBABILITY FOR EACH EVASION BY SOLVING CIRCULAR CCVERAGE	2160
C	FUNCTION.	2170
	CALL GCIP(D,AKILL,PK)	2180
	PPK(N)=PK	2190
	SUMM=SUMM+PPK(N)*UNU(N)	2200
500	SUM=SUM+PPK(N)	2210
C	COMPUTE PROBABILITY FOR EVASIVE SUBMARINE USING WEIGHTED PROBAPILITIES	2220
	WTPAVG=SUMM/UN	2230
	PAVG=SUM/UN	2240
C	COMPUTE PROBABILITY ASSUMING SUBMARINE NOT ALERTED OF VEHICLES	2250
C	PRESEANCE.	2260
	SUMUNU=0.0	2270
	DO 502 N=1,NUN	2280
502	SUMUNU=SUMUNU+UNU(N)	2290
C	LAST KNOWN POSITION OF SUBMARINE IS THE ORIGIN. PREDICTED SUBMARI	2300
C	NE POSITION AFTER BLIND TIME (WITH NO EVASION) IS (XX,YY). CCMPUTE	2310
C	POSITIONS OF CENTERS OF CELLS.	2320
	SUM=0.	2330
	DO 600 I=1,5	2340
	TB=SAVE	2350
	VV=(SLI-AA(I)*SUERR)*TB	2360
	DO 600 J=1,5	2370
	THETER=AA(J)*STHDEL	2380
	SUBX(I,J)=VV*COSF(THETER)	2390
	SUBY(I,J)=VV*SINF(THETER)	2400

```

XSUB=SUBX(I,J)
YSUB=SUBY(I,J)
SBIAS(I,J)=SORTF((XX-XSUB)**2+(YY-YSUB)**2)
D=SBIAS(I,J)/SIGJT
AKILL=EXPRNG/SIGJT
CALL CCIP(D,AKILL,PK)
600 SUM=SUM+PK
PROB=SUM*.04
GO TO 3010
C PROB IS PROBABILITY THAT VEHICLE RELOCATES SLB AT DATUM IF SLB
C DOES NOT EVADE
C PRINT OUT INPUT PARAMETER SET
1999 WRITE OUTPUT TAPE 3,2001,M,NEXT,NO
2001 FORMAT(1H1,/,5X,1CHOUTPUT RUN ,13,1X,2HOF,13,79X,5HPAGE ,13)
WRITE OUTPUT TAPE 3,2005
2005 FORMAT(1H0,46X,28HCOMPLETE INPUT PARAMETER SET)
WRITE OUTPUT TAPE 3,2010
2010 FORMAT(///,20X,9HPARAMETER,11X,5HVALUE,15X,7HMEANING)
WRITE OUTPUT TAPE 3,2015,U1
2015 FORMAT(///,20X,2HU1,18X,F10.4,10X,30HSUBMARINE CRUISE SPEED (KNOTS
1))
WRITE OUTPUT TAPE 3,2020,U2
2020 FORMAT(/ ,20X,2HU2,18X,F10.4,10X,30HSUBMARINE SILENT SPEED (KNCTS)
1)
WRITE OUTPUT TAPE 3,2025,U3
2025 FORMAT(/ ,20X,2HU3,18X,F10.4,10X,28HSUBMARINE FAST SPEED (KNCTS))
WRITE OUTPUT TAPE 3,2030,Z
2030 FORMAT(/ ,20X,1HZ,19X,F10.4,10X,57HVEHICLE TRANSIT SPEED TO DATUM
1(NEGLECT ACCEL. OR DECEL.))
WRITE OUTPUT TAPE 3,2035,PTOT
2035 FORMAT(/ ,20X,4HPTOT,16X,F10.4,10X,23HPRE TAKE OFF TIME (MIN))
WRITE OUTPUT TAPE 3,2040,TOT
2040 FORMAT(/ ,20X,3HTOT,17X,F10.4,10X,19HTAKE OFF TIME (MIN))
WRITE OUTPUT TAPE 3,2045,CLDT
2045 FORMAT(/ ,20X,4HCLDT,16X,F10.4,10X,15HLAND TIME (MIN))
WRITE OUTPUT TAPE 3,2050,RELT
2050 FORMAT(/ ,20X,4HRELT,16X,F10.4,10X,28HTARGET RELOCATION TIME (MIN)
1)
WRITE OUTPUT TAPE 3,2055,T1
2055 FORMAT(/ ,20X,2HT1,18X,F10.4,10X,38HELLAPSED TIME CF SUB AT SPEED
1U3 (MIN))
WRITE OUTPUT TAPE 3,2060,THETA
2060 FORMAT(/ ,20X,5HTHETA,15X,F10.4,10X,46HCOURSE CF SUB AT LAST KNOWN
1 POSITION (DEGREES))
WRITE OUTPUT TAPE 3,2065,BETA
2065 FORMAT(/ ,20X,4HBETA,16X,F10.4,10X,42HTRUE BEARING CF SUB FROM VEH
1ICLE (DEGREES))
WRITE OUTPUT TAPE 3,2070,RAI

```

```

241C
2420
2430
2440
2450
2460
2470
248C
2490
2500
2510
2520
2530
2540
255C
2560
2570
2580
259C
2600
2610
2620
2630
2640
2650
2660
2670
2680
2690
2700
2710
2720
2730
2740
2750
2760
277C
2780
2790
2800
2810
2820
2830
2840
2850
2860
2870
288C

```



```

2070 FORMAT(/ ,20X,3HRAI,17X,F10.4,10X,56HRANGE TO SUB AT LAST KNOWN PO
POSITION FROM VEHICLE (MILES))
WRITE OUTPUT TAPE 3,2080,TR
2080 FORMAT(/ ,20X,2HTR,18X,F10.4,10X,27HTURNING RADIUS OF SUB (YDS))
WRITE OUTPUT TAPE 3,2085,PRCNTN
2085 FORMAT(/ ,20X,6HPRCNTN,14X,F10.4,10X,37HNAV. ERROR IN PERCENT DIST
ANCE TO SUB)
WRITE OUTPUT TAPE 3,2090,PRCNTS
2090 FORMAT(/ ,20X,6HPRCNTS,14X,F10.4,10X,42HSENSOR RANGE ERROR IN PERC
ENT SENSOR RANGE)
WRITE OUTPUT TAPE 3,2095,BRGER
2095 FORMAT(/ ,20X,5HBRGER,15X,F10.4,10X,31HSENSOR BEARING ERROR IN DEG
REES)
WRITE OUTPUT TAPE 3,2100,EXPRNG
2100 FORMAT(/ ,20X,6HEXPNG,14X,F10.4,10X,58HRANGE EXPECTED FROM SENSO
R FOR LOCALIZATION AT DATUM, MILES)
WRITE OUTPUT TAPE 3,2105,PSI
2105 FORMAT(/ ,20X,3HPSI,17X,F10.4,10X,42HLEFT BOUND FOR SUB EVASIVE TU
RN IN DEGREES)
WRITE OUTPUT TAPE 3,2110,DELTAL
2110 FORMAT(/ ,20X,6HDELTAL,14X,F10.4,10X,43HRIGHT BOUND FOR SUB EVASIV
E TURN IN DEGREES)
WRITE OUTPUT TAPE 3,2115,NU
2115 FORMAT(/ ,20X,2HNU,18X,15,15X,47HNUMBER INCREMENTS CONSIDERED IN P
SI-DELTA RANGE)
WRITE OUTPUT TAPE 3,2120,NEXT
2120 FORMAT(/ ,20X,4HNEXT,16X,15,15X,28HNUMBER OF SETS OF INPUT DATA)
WRITE OUTPUT TAPE 3,2125,UERR
2125 FORMAT(/ ,20X,4HUERR,16X,F10.4,10X,29HSUBMARINE SPEED ERROR (KNOTS
))
WRITE OUTPUT TAPE 3,2130,THDEL
2130 FORMAT(/ ,20X,5HTHDEL,15X,F10.4,10X,32HSUBMARINE COURSE ERROR (DEG
REES))
)))
NO=NO+1
GO TO 40
9050 WRITE OUTPUT TAPE 3,9055,M,NEXT,NO
9055 FORMAT(1H1,///,5X,11HOUTPUT RUN ,13,1X,2HOF,13,79X,5HPAGE ,13,///
1,5X,67HERROR. INCORRECT SOLUTION BEING CALCULATED. CONTINUE WITH N
EXT RUN.)
NO=NO+1
M=M+1
GO TO 20
3010 WRITE OUTPUT TAPE 3,3015,M,NEXT,NO
3015 FORMAT(1H1,///,5X,1CHOUTPUT RUN ,13,1X,2HOF,13,79X,5HPAGE ,13)
WRITE OUTPUT TAPE 3,3020
3020 FORMAT(///,50X,16HINPUT PARAMETERS)
WRITE OUTPUT TAPE 3,3025,Z,PTOT,TOT,CLODT,RELT,U1,U2,U3,RAI,THETA

```

```

2890
2900
2940
2950
2960
2970
2980
2990
3000
3010
3020
3030
3040
3050
3060
3070
3080
3090
3100
3110
3120
3130
3140
3150
3160
3170
3180
3190
3200
3210
3220
3230
3240
3250
3260
3270
3280
3290
3300
3310
3320
3330
3340
3350
3360
3370
3380
3390

```



```

3025 FORMAT(///,46X,56HTARGET SUBMARINE SUBMARINE SUBMARINE S
SUBMARINE//1H,5X,110HVEHICLE PRE TAKE TAKE OFF LAND RELOCAT
2ION CRUISE SILENT FAST TO VEHICLE SUBMARINE/1
3H,6X,106HSPEED OFF TIME TIME TIME TIME SPEE
4D SPEED SPEED RANGE CCURSE//1H,5X,110H(KNO
5TS) (MIN) (MIN) (MIN) (MIN) (KNOTS) (KNOT
6S) (KNOTS) (MILES) (DEGREES)//1H,6X,F6.2,2X,F6.2,6X,F
76.2,3X,F6.2,3X,F6.2,6X,F6.2,7X,F6.2,6X,F6.2,6X,F6.2,7X,F6.2)
WRITE OUTPUT TAPE 3,3030,DETA,PRCNTN,PRCNTS,BRGER,EXPRNG
3030 FORMAT(///,49X,32HSENSOR EXPECTED//1H,20X,61HTRUE
1 BEARING NAVIGATION RANGE ERROR SENSOR RANGE OF//1H,21X,
263HSUP FROM ERROR ERROR BEARING LOCALIZATION
3//1H,23X,59HVEHICLE (PERCENT (PERCENT ERROR S
4ENSOR//1H,21X,59H(DEGREES) DISTANCE) RANGE) (DEGREES)
5 (MILES)//1H,22X,F6.2,9X,F6.2,6X,F5.2,7X,F6.2,6X,F6.2)
IF(IX)9050,3034,3333
3333 WRITE OUTPUT TAPE 3,3032
3032 FORMAT(///,10X,105H** NOTE-RANGE TO SUB IS CLOSE ENOUGH FOR SUB TO
1 CLOSE VEHICLE AND FIRE WEAPONS BEFORE VEHICLE CAN ESCAPE.)
3034 CONTINUE
WRITE OUTPUT TAPE 3,3035,NUN,PAVG
3035 FORMAT(///,30X,32HAVERAGE SUCCESS PROBABILITY FOR ,12,20H EVASION
1TACTICS IS ,F5.3)
IF(SUMUNU)9050,3036,3031
3036 WRITE OUTPUT TAPE 3,3037
3037 FORMAT(///,30X,45HAVERAGE WEIGHTED SUCCESS PROBABILITY NOT USED)
GO TO 3039
3031 WRITE OUTPUT TAPE 3,3038,NUN,WTPAVG
3038 FORMAT(///,21X,41HAVERAGE WEIGHTED SUCCESS PROBABILITY FOR ,12,20H
1EVASION TACTICS IS ,F5.3)
3039 WRITE OUTPUT TAPE 3,3041,PROB
3041 FORMAT(///,42X,39HCOMPUTED VALUES FOR UNALERTED SUBMARINE//1H,30-
1X,28HAVERAGE SUCCESS PROBABILITY ,F5.3)
WRITE OUTPUT TAPE 3,3040
3040 FORMAT(///,42X,37HCOMPUTED VALUES FOR SUBMARINE EVASION//1H,62
1X,37HBLIND DISTANCE TRANSIT RELATIVE//1H,17X,94HEVASION
2EVASION TURN SUCCESS TIME TC DATUM SPE
3CD SIG TOTAL//1H,17X,94HNUMBER (DEGREES) PROBABILI
4TY (MIN) (MILES) (KNOTS) (MILES)//
DO 3055 N=1,NUN
WRITE OUTPUT TAPE 3,3050,N,DELTA(N),PPK(N),TB,DISDAT,RSPD,SIGJT
3050 FORMAT(/1H,16X,15,9X,F8.2,10X,F5.3,8X,F6.2,6X,F6.2,11X,F6.2,6X,F5
1.2)
3055 CONTINUE
NO=NO+1
M=M+1
GO TO 20
9000 END

```

```

SUBROUTINE INPUT(U1,U2,U3,Z,PTOT,TOT,CLDT,RELT,T1,THETA,BETA,RAI,
1 TR,PRCNTN,PRCNTS,BRGER,EXPRNG,PSI,UERR,THDEL,NU,NEXT,DELTAL,SUM
2,AA,IFLAG,UNU,DELN,SUMM,M)
DIMENSION AA(5),UNU(15)
SUM=0.
SUMM=0.
IFLAG=0
DELN=C.
IF(M-1)111,91,93
91 READ 110,U1
   READ 110,U2
   READ 110,U3
   READ 110,Z
   READ 110,PTOT
   READ 110,TOT
   READ 110,CLDT
   READ 110,RELT
   READ 110,T1
   READ 110,THETA
   READ 110,BETA
   READ 110,RAI
   READ 110,TR
   READ 110,PSI
   READ 110,DELTAL
   READ 110,BRGER
   READ 110,EXPRNG
   READ 110,PRCNTN
   READ 110,PRCNTS
   READ 110,THDEL
   READ 110,UERR
110 FORMAT(F12.4)
   READ 112,NU
   READ 112,NEXT
112 FORMAT(I4)
   READ 113,(AA(I),I=1,5)
113 FORMAT(5F12.4)
   NUN=NU+1
   READ 114,(UNU(N),N=1,NUN)
114 FORMAT(12F6.4)
   GO TO 111
93 READ 94,IJK
   94 FORMAT(I4)
   GO TO(1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,23,
1 24,25,26,27),IJK
1 READ 110,U1
   GO TO 93
2 READ 110,U2
   GO TO 93

```

```

3860
3870
3880
3890
3900
3910
3920
3930
3940
3950
3960
3970
3980
3990
4000
4010
4020
4030
4040
4050
4060
4080
4090
4100
4110
4120
4130
4140
4150
4160
4170
4180
4190
4200
4210
4220
4230
4240
4250
4260
4270
4280
4290
4300
4310
4320
4330
4340

```



```

3 READ 110,U3
GO TO 93
4 READ 110,Z
GO TO 93
5 READ 110,PTOT
GO TO 93
6 READ 110,TOT
GO TO 93
7 READ 110,CLDT
GO TO 93
8 READ 110,RELT
GO TO 93
9 READ 110,T1
GO TO 93
10 READ 110,THETA
GO TO 93
11 READ 110,BETA
GO TO 93
12 READ 110,RAI
GO TO 93
C THIS SPACE FREE FOR AN INPUT VARIABLE
13 GO TO 93
14 READ 110,TR
GO TO 93
15 READ 110,PSI
GO TO 93
16 READ 110,DELTAL
GO TO 93
17 READ 110,BRGER
GO TO 93
18 READ 110,EXPRNG
GO TO 93
19 READ 110,PRCNTN
GO TO 93
20 READ 110,PRCNTS
GO TO 93
21 READ 110,THDEL
GO TO 93
22 READ 110,UERR
GO TO 93
23 READ 112,NU
NUN=NU+1
GO TO 93
24 READ 112,NEXT
GO TO 93
25 READ 113,(AA(I),I=1,5)
GO TO 93
26 READ 114,(UNU(N),N=1,NUN)

```

```

4350
4360
4370
4380
4390
4400
4410
4420
4430
4440
4450
4460
4470
4480
4490
4500
4510
4520
4530
4540
4550
4560
4570
4580
4590
4600
4610
4620
4630
4640
4650
4660
4670
4680
4690
4700
4710
4720
4730
4740
4750
4760
4770
4780
4790
4800
4810
4820

```



```

GO TO 93
27 GO TO 111
111 RETURN
END
SUBROUTINE OCIP(A,V,PAV)
IF(V-A-5.0)1,1,2
2 PAV=1.C
RETURN
1 IF(V-A+5.0)3,4,4
3 PAV=0.0
RETURN
4 PI=3.14159265
HALPI=PI*0.5
TWPI=2.0*PI
RTWPI=SQRTF(TWPI)
RHAPI=SQRTF(HALPI)
IF(A-4.)5,6,6
C A LESS THAN FOUR
5 ASQ=A*A
AFOUR=ASQ*ASQ
ASIX=AFOUR*ASQ
Z=-ASQ*0.25
EXP=EXPF(Z)
CALL IZERO(-Z,BESSZ)
CALL ICNE(-Z,BESSO)
EM1P=RHAPI*EXP*(BESSZ+ASQ*(BESSZ+BESSO)*0.5)
EM3P=RHAPI*EXP*((ASQ+3.0)*BESSZ+(AFOUR+4.C*ASQ)*(BESSZ+BESSO)*0.5)
EM5P=RHAPI*EXP*((AFOUR+11.C*ASQ+15.0)*BESSZ+(ASIX+12.0*AFOUR+23.0*
1 ASQ)*(BESSZ+BESSO)*C.5)
EM2P=ASQ+2.0
EM4P=AFOUR+8.C*ASQ+8.0
EM6P=ASIX+18.0*AFOUR+72.C*ASQ+48.0
SIGSQ=EM2P-(EM1P**2)
SIGMA=SQRTF(SIGSQ)
EM1P2=EM1P**2
EM1P3=EM1P*EM1P2
EM1P4=EM1P2**2
EM1P5=EM1P4*EM1P
EM1P6=EM1P3**2
EM3=EM3P-3.0*EM1P*EM2P+2.0*EM1P3
EM4=EM4P-4.0*EM1P*EM3P+6.0*EM1P2*EM2P-3.0*EM1P4
EM5=EM5P-5.0*EM1P*EM4P+10.0*EM1P2*EM3P-10.C*EM1P3*EM2P+4.0*EM1P5
EM6=EM6P-6.0*EM1P*EM5P+15.0*EM1P2*EM4P-20.0*EM1P3*EM3P+15.0*EM1P4*
1 EM2P-5.0*EM1P6
TERM1=EM3/(SIGMA*SIGSQ)
TERM2=EM4/(SIGSQ**2)-3.0
TERM3=EM5/(SIGSQ**2*SIGMA)-10.0*EM3/(SIGMA*SIGSQ)
TERM4=EM6/(SIGSQ**3)-15.C*EM4/(SIGSQ**2)+30.0

```

```

483C
484C
4850
4860
487C
4880
4890
490C
491C
4920
4930
4940
4950
4960
4970
498C
4990
5000
5010
502C
5030
5040
505C
506C
5070
508C
5090
5100
5110
5120
5130
5140
5150
516C
5170
5180
5190
520C
5210
5220
5230
5240
5250
5260
527C
5280
5290
5300

```

```

6      GO TO 7
      ASQ=A*A
      ACUBE=A*ASQ
      AF0UR=ASQ**2
      AFIVE=AF0UR*A
      ASIX=ACUBE**2
      ASVEN=ASIX*A
      EM1P=A+0.5/A+1.0/(8.0*ACUBE)+3.0/(16.0*AFIVE)+75.0/(128.0*ASVEN)
      SIGMA=1.0-1.0/(4.0*ASQ)-9.0/(32.0*AF0UR)-97.0/(128.0*ASIX)
      TERM1=1.0/ACUBE+3.0/AFIVE
      TERM2=-3.0/AF0UR
      TERM3=C.0
      TERM4=C.0
7      WHY=(V-EM1P)/SIGMA
      WHY2=WHY**2
      WHY3=WHY*WHY2
      WHY4=WHY2**2
      WHY5=WHY*WHY4
      CALL PHI(WHY,W,ERF,CPHI)
      PAV=CPHI-(EXP(-WHY2*0.5)/RTWPI)*((WHY2-1.0)/6.0*TERM1+(WHY3-3.0*
1      WHY)/24.0*TERM2+(WHY4-6.0*WHY2+3.0)/120.0*TERM3+(WHY5-10.0*WHY3
      2+15.0*WHY)/720.0*TERM4)
      RETURN
      END
      SUBROUTINE PHI(WHY,W,ERF,CPHI)
      W=ABS(WHY)/SQRT(2.0)
      CALL ERRORR(W,ERF)
      IF(WHY-0.000001)500,601,600
600    CPHI=C.5*(1.0+(WHY/ABS(WHY))*ERF)
      RETURN
601    CPHI=C.5
      END
      SUBROUTINE ERRORR(W,ERF)
      P=(((0.00328975*W-0.00039446)*W+0.02743349)*W+0.08864027)*W +
1      0.14112821)*W+1.0
      P=P*P
      P=P*P
      P=P*P
      ERF=1.0-1.0/P
      RETURN
      END
      SUBROUTINE IZERO(EX,BESSZ)
      BESSZ=1.0
      EXSQ=EX*EX
      DENOM=1.0
      XNUM=EXSQ/4.0
      FNUM=1.0
      DO 100 I=1,10

```

```

5310
5320
5330
5340
5350
5360
5370
5380
5390
5400
5410
5420
5430
5440
5450
5460
5470
5480
5490
5500
5510
5520
5530
5540
5550
5560
5570
5580
5590
5600
5610
5620
5630
5640
5650
5660
5670
5680
5690
5700
5710
5720
5730
5740
5750
5760
5770
5780

```

```

      D=I
      FNUM=FNUM*XNUM
      DENOM=DENOM*D
100  BESSZ=BESSZ+(FNUM/(DENOM**2))
      END
      SUBROUTINE IONE(EX,BESSO)
      BESSO =1.0
      EXSQ=EX*EX
      DEN1=1.0
      DEN2=1.0
      XNUM=EXSQ/4.0
      FNUM=1.0
      DO 101 I=1,10
      D=I
      FNUM =FNUM*XNUM
      DEN1=DEN1*D
      DEN2=DEN2*(D+1.0)
101  BESSO=BESSO +FNUM/(DEN1*DEN2)
      BESSO =BESSO*EX*0.5
      END
      END

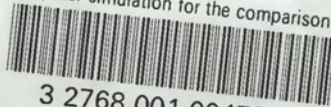
```

```

5790
5800
5810
5820
5830
5840
5850
5860
5870
5880
5890
5900
5910
5920
5930
5940
5950
5960
5970
5980
5990

```


thesD69
Computer simulation for the comparison o



3 2768 001 00472 4
DUDLEY KNOX LIBRARY